

Mastery Checklist

Geometric Sequence & Series

In order to prove Mastery for this concept you must be able complete the following all by **yourself**. No help from Notes, Partners or Teacher. Use all other problems to practice and test yourself with the following:

- Complete # 10 & 13 on "Geometric Sequence" worksheet
- Complete # 11, 16 & 17 on "Geometric Series" worksheet
- Complete # 16, 19 & 20 on " Cloud and Star" worksheet
- Complete a Mind Map on how the Concept of Geometric Series and Sequence is connected.

Mind Map

Geometric Series & Sequence

Task 1:

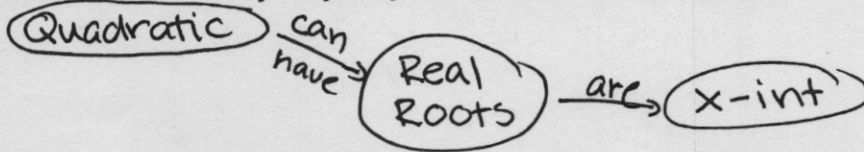
Review your notes/Quick Check/Unit 5 Test and write down all key ideas/concepts/vocabulary/examples for LT: 5B

Task 2:

Group and Connect all your concepts together

Task 3:

Label each Connection by why they are connected. For example:



Task 4:

Add in examples and visuals where they fit.

Task 5:

Review Checklist below and make sure that your Mind Map contains everything you need.

- Contains all of these Concepts/Vocabulary

Geometric Sequence

Geometric Series

Sigma Notation

General Term

Sum

Common Ratio

Nth term

Elements

Formula

Definition

- All Connections are labeled
- Contains Example Problems
- Contains Visuals
- Review Mind Map on the Backside and see if you need to adjust or add anything.

What is missing?
How can you make this better?

Ex: $3, 6, 12, 24, \dots$
 $a_1 = 3$ first term
 $r = 2$ common ratio

List of elements which are created by mult. the previous term "a" a common ratio "r"

Geometric Sequence

~~Geometric Sequence~~
 $a_1, a_1 r, a_1 r^2, \dots$
 $a_1 =$ first term
 $r =$ common ratio

general term
 $a_n = a_1 r^{n-1}$

used to find n th term

sum of n -terms of a sequence

Geometric Series

way to represent it

need to find

sigma notation

$$\sum_{n=1}^5 a_1 r^{n-1} = S_5$$

need to remember

to write a series in sigma notation

Ex 1

$$\sum_{n=1}^6 (-3)^{n-1} (-2)^{n-1}$$

first term a_1
 $r =$ common ratio

when

$$S_n = \frac{a_1(1-r^n)}{1-r}$$

to find sum

$a_1 =$ first term

used to find the sum of n terms

$r =$ common ratio

LT: 5B Geometric Sequence

Determine if the sequence is geometric. If it is, find the common ratio.

1) $-1, 6, -36, 216, \dots$

2) $-1, 1, 4, 8, \dots$

3) $4, 16, 36, 64, \dots$

4) $-3, -15, -75, -375, \dots$

5) $-2, -4, -8, -16, \dots$

6) $1, -5, 25, -125, \dots$

Given the explicit formula for a geometric sequence find the first five terms and the 8th term.

7) $a_n = 3^{n-1}$

8) $a_n = 2 \cdot \left(\frac{1}{4}\right)^{n-1}$

9) $a_n = -2.5 \cdot 4^{n-1}$

10) $a_n = -4 \cdot 3^{n-1}$

Given the following geometric sequence find the general term or nth term.

11.) $-3, -9, -27, \dots$

12.) $6, -3, \frac{3}{2}, -\frac{3}{4}, \dots$

13.) $2, 6, 18, 54, \dots$

14.) $-4, 16, -64, \dots$

Answer key

LT: 5B Geometric Sequence

Determine if the sequence is geometric. If it is, find the common ratio.

1) -1, 6, -36, 216, ...

$$r = -6$$

2) -1, 1, 4, 8, ...

Not Geometric

3) 4, 16, 36, 64, ...

Not Geometric

4) -3, -15, -75, -375, ...

$$r = 5$$

5) -2, -4, -8, -16, ...

$$r = 2$$

6) 1, -5, 25, -125, ...

$$r = -5$$

Given the explicit formula for a geometric sequence find the first five terms and the 8th term.

7) $a_n = 3^{n-1}$

1st 5 terms: 1, 3, 9, 27, 81

$$a_8 = 2187$$

8) $a_n = 2 \cdot \left(\frac{1}{4}\right)^{n-1}$

2, $\frac{1}{2}$, $\frac{1}{8}$, $\frac{1}{32}$, $\frac{1}{128}$

$$a_8 = \frac{1}{8192}$$

9) $a_n = -2.5 \cdot 4^{n-1}$

-2.5, -10, -40, -160, -640

$$a_8 = -40960$$

10) $a_n = -4 \cdot 3^{n-1}$

-4, -12, -36, -108, -324

$$a_8 = -8748$$

Given the following geometric sequence find the general term or nth term.

11.) -3, -9, -27, ...

$$a_n = -3(3)^{n-1}$$

12.) 6, -3, $\frac{3}{2}$, $-\frac{3}{4}$, ...

$$a_n = 6\left(-\frac{1}{3}\right)^{n-1}$$

13.) 2, 6, 18, 54, ...

$$a_n = 2(3)^{n-1}$$

14.) -4, 16, -64, ...

$$a_n = -4(-4)^{n-1} = -4^1 \cdot (-4)^{n-1} = -4^n$$

↑ ↑ since it has the same base it could be simplified.

LT: 5B Geometric Series

Evaluate each geometric series described.

$$5) \sum_{k=1}^7 4^{k-1}$$

$$6) \sum_{i=1}^8 (-6)^{i-1}$$

$$7) \sum_{i=1}^9 2^{i-1}$$

$$8) \sum_{m=1}^9 -2^{m-1}$$

$$9) \sum_{n=1}^8 2 \cdot (-2)^{n-1}$$

$$10) \sum_{n=1}^9 4 \cdot 3^{n-1}$$

$$11) \sum_{n=1}^{10} 4 \cdot (-3)^{n-1}$$

$$12) \sum_{n=1}^9 (-2)^{n-1}$$

$$13) 1 + 2 + 4 + 8 \dots, n = 6$$

$$14) 2 - 10 + 50 - 250 \dots, n = 8$$

$$15) 1 - 4 + 16 - 64 \dots, n = 9$$

$$16) -2 - 6 - 18 - 54 \dots, n = 9$$

$$17) 1 - 5 + 25 - 125 \dots, n = 7$$

$$18) -3 - 6 - 12 - 24 \dots, n = 9$$

Answer key

LT: 5B Geometric Series

Evaluate each geometric series described.

$$5) \sum_{k=1}^7 4^{k-1} = 5461$$

$$6) \sum_{i=1}^8 (-6)^{i-1} = -239945$$

$$7) \sum_{i=1}^9 2^{i-1} = 511$$

$$8) \sum_{m=1}^9 -2^{m-1} = -511$$

$$9) \sum_{n=1}^8 2 \cdot (-2)^{n-1} = 170$$

$$10) \sum_{n=1}^9 4 \cdot 3^{n-1} = 39364$$

$$11) \sum_{n=1}^{10} 4 \cdot (-3)^{n-1} = 59048$$

$$12) \sum_{n=1}^9 (-2)^{n-1} = \del{171} = 171$$

$$13) 1 + 2 + 4 + 8 \dots, n = 6$$

$$S_6 = 63$$

$$14) 2 - 10 + 50 - 250 \dots, n = 8$$

$$S_8 = -130208$$

$$15) 1 - 4 + 16 - 64 \dots, n = 9$$

$$S_9 = 52429$$

$$16) -2 - 6 - 18 - 54 \dots, n = 9$$

$$S_9 = -19682$$

$$17) 1 - 5 + 25 - 125 \dots, n = 7$$

$$S_7 = 13021$$

$$18) -3 - 6 - 12 - 24 \dots, n = 9$$

$$S_9 = -1533$$

Directions: Start with the bottom left cloud. Follow the arrows. When you get to a large star problem find the *** problem around the room. Complete your work and thinking on a dry-erase board and leave work to be checked by Ms. Mirzaian.

Try one of the following *** problems (Pink/Green) Leave your work and thinking on a big board to be checked.

- Determine the number of terms (n) in each geometric series
- 17.) $a_1 = -2, r = 5, S_n = -62$
 18.) $a_1 = -3, r = 4, S_n = -4095$
 19.) $a_3 = 27, r = -3, S_n = -60$
 20.) $a_1 = -3, r = -2, S_n = 63$

Try one of the following *** problems (Blue/Orange) Leave your work and thinking on a big board to be checked.

Evaluate the following Geometric Series:

- 13.) $\sum_{n=1}^9 4 \cdot 3^{n-1}$
 14.) $\sum_{n=1}^8 2 \cdot (-2)^{n-1}$
 15.) $1+2+4+8\dots, n=6$
 16.) $1-4+16-64\dots, n=9$

State the first 6 terms in the sequence described below:

- 11.) $\sum_{i=1}^8 (-6)^{i-1}$
 12.) $\sum_{n=1}^8 2 \cdot (-2)^{n-1}$

Complete the Yellow *** Problem. Leave your work on the wall for Ms Mirzaian to check. Once you are done move on to the next one star cloud.

Start Here

Determine if the sequence is geometric. If it is, find the common ratio.

1) $-1, 6, -36, 216, \dots$

2) $-1, 1, 4, 8, \dots$

3) $4, 15, 36, 64, \dots$

4) $-3, -15, -75, -375, \dots$

Find the general formula for the following geometric sequences:

7.) $1, 3, 9, 27, 81$

8.) $-2.5, 10, -40, 160$

9.) $2, \frac{1}{2}, \frac{1}{8}, \frac{1}{32}, \dots$

10.) $-4, -12, -36, -108, \dots$

Answer Key:

- 1.) $r=-6$
- 2.) Not geometric
- 3.) Not geometric
- 4.) $R=5$
- 5.) $R=2$
- 6.) $R=-5$
- 7.) $a_n = (1)3^{n-1}$
- 8.) $a_n = -2.5(-4)^{n-1}$
- 9.) $a_n = 2\left(\frac{1}{4}\right)^{n-1}$
- 10.) $a_n = -4(3)^{n-1}$
- 11.) 1, -6, 36, -216, 1296, -7776
- 12.) 2, -4, 8, -16, 32, -64
- 13.) 39364
- 14.) -170
- 15.) 63
- 16.) 52429
- 17.) $n=3$
- 18.) $n=6$
- 19.) $n=4$
- 20.) $n=6$