

You must do your work on a separate piece of paper.

Find the exact value of the expression.

1. $\cos 105^\circ$

2. $\sin 195^\circ$

3. $\tan 165^\circ$

4. $\tan \frac{\pi}{12}$

5. $\sin \frac{7\pi}{12}$

6. $\cos \frac{11\pi}{12}$

Evaluate the expression given $\cos u = \frac{4}{5}$; $0 \leq u < \frac{\pi}{2}$; and $\tan v = \frac{8}{15}$; $\pi < v < \frac{3\pi}{2}$

7. $\sin(u+v)$

8. $\cos(u+v)$

9. $\tan(u+v)$

10. $\sin(u-v)$

11. $\cos(u-v)$

12. $\tan(u-v)$

Simplify the expression.

13. $\sin(x-2\pi)$

14. $\tan\left(x - \frac{3\pi}{4}\right)$

15. $\cos \frac{\pi}{4} \cos \frac{\pi}{3} - \sin \frac{\pi}{4} \sin \frac{\pi}{3}$

16. $\sin 20^\circ \cos 50^\circ + \cos 20^\circ \sin 50^\circ$

17. $\frac{\tan 78^\circ - \tan 42^\circ}{1 + \tan 78^\circ \tan 42^\circ}$

18. $\frac{\tan \frac{5\pi}{3} + \tan \frac{\pi}{4}}{1 - \tan \frac{5\pi}{3} \tan \frac{\pi}{4}}$

Verify the identity.

19. $\cos(u+v) + \cos(u-v) = 2\cos u \cos v$

20. $\sin(u+v) - \sin(u-v) = 2\cos u \sin v$

Simplify as far as possible.

21. $(\sin x + \cos x)^2$

22) $\frac{\sin 2x}{\sin x}$

23) $4\sin \frac{x}{2} \cos \frac{x}{2}$

24. $\cos^4 x - \sin^4 x$

25. $\frac{1}{2} \sin 3x \cos 3x$

26) $\frac{\cos 2x}{\cos^2 x}$

Solve the equation for $0 \leq x < 2\pi$

27. $\cos 2x = \cos x$

28. $\sin 2x \sin x = \cos x$

29. $\cos 2x = -\sin x$

30. $\sin 2x + \sqrt{2} \sin x = 0$

31. $\cos 2x - \cos x = 2$

32. $\tan(x - 10^\circ) = 1; 0 \leq x < 360^\circ$

Use a double-angle or half angle identity to find the exact value of each expression.

$$\sin \theta = \frac{8}{17} \text{ and } 90^\circ < \theta < 180^\circ.$$

33. $\cos 2\theta$

34. $\sin 2\theta$

35. $\tan 2\theta$

36. $\sin\left(\frac{\theta}{2}\right)$

37. $\cos\left(\frac{\theta}{2}\right)$

38. $\tan\left(\frac{\theta}{2}\right)$

Answers:

1. $\frac{\sqrt{2} - \sqrt{6}}{4}$

2. $\frac{\sqrt{2} - \sqrt{6}}{4}$

3. $-2 + \sqrt{3}$

4. $2 - \sqrt{3}$

5. $\frac{\sqrt{2} + \sqrt{6}}{4}$

6. $\frac{-\sqrt{2} - \sqrt{6}}{4}$

7. $-77/85$

8. $-36/85$

9. $77/36$

10. $-13/85$

11. $-84/85$

12. $13/84$

13. $\sin x$

14. $\frac{\tan x + 1}{1 - \tan x}$

15. $\cos \frac{7\pi}{12}$

16. $\sin 70^\circ$

17. $\tan 36^\circ$

18. $\tan \frac{23\pi}{12}$

21. $1 + \sin 2x$

22. $2 \cos x$

23. $2 \sin x$

24. $\cos 2x$

25. $\frac{1}{4} \sin(6x)$

26. $2 - \sec^2 x$

27. $0; \frac{2\pi}{3}; \frac{4\pi}{3}$

28. $\frac{\pi}{4}; \frac{\pi}{2}; \frac{3\pi}{4}; \frac{5\pi}{4}; \frac{3\pi}{2}; \frac{7\pi}{4}$

29. $\frac{\pi}{2}; \frac{7\pi}{6}; \frac{11\pi}{6}$

30. $0; \frac{3\pi}{4}; \pi; \frac{5\pi}{4}$

31. π

32. $55^\circ; 235^\circ$

33. $161/289$

34. $-240/289$

35. $-240/161$

36. $\frac{4\sqrt{17}}{17}$

37. $\frac{\sqrt{17}}{17}$

38. 4