

Do your work on a separate piece of paper for full credit.

Worksheet 14.6 – 14.7

1. If A is acute;  $\sin A = \frac{15}{17}$ , find  $\tan 2A$ .
2. If A is acute;  $\tan A = \frac{5}{12}$ , find  $\cos 2A$
3. If  $\pi < A < \frac{3\pi}{2}$ ;  $\tan A = \frac{5}{12}$ , find  $\cos \frac{A}{2}$
4. If A is acute;  $\cos A = \frac{1}{4}$ , find  $\sin 2A$
5. If  $\frac{3\pi}{2} < A < 2\pi$ ;  $\cos A = \frac{1}{4}$ , find  $\sin \frac{A}{2}$
6. Simplify completely.  
 $\cos\left(\frac{\pi}{3} + x\right) - \cos\left(\frac{\pi}{3} - x\right)$
7. Evaluate  $\tan\left(\frac{3\pi}{4} - \theta\right)$  when  $\tan \theta = \frac{1}{3}$
8. Suppose that  $\sin \alpha = \frac{3}{5}$  and  $\sin \beta = \frac{24}{25}$ , where  $0 < \alpha < \frac{\pi}{2} < \beta < \pi$ . Find  $\sin(\alpha + \beta)$
9. Suppose that  $\sin \alpha = \frac{4}{5}$  and  $\sin \beta = \frac{1}{2}$  where  $\frac{\pi}{2} < \alpha < \beta < \pi$ . Find  $\sin(\alpha - \beta)$
10. Given :  $\tan \alpha = \frac{2}{3}$  and  $\tan \beta = \frac{1}{2}$ . Find  $\tan(\alpha + \beta)$
11. Simplify  $12 \sin 4x \cos 4x$
12. Find the exact value of  $\cos 285^\circ$  using sum/different formulas.
13. Find the exact value of  $\sin 105^\circ$  using half angle formulas.
14. Find the exact value of  $\sin \frac{17\pi}{12}$
15. Find the exact value of  $\cos \frac{13\pi}{12}$

Given  $\sin u = \frac{-5}{13}$ ,  $\frac{3\pi}{2} < u < 2\pi$ , find the exact value of the expression.

16.  $\sin \frac{u}{2}$
17.  $\cos \frac{u}{2}$
18.  $\tan \frac{u}{2}$
19.  $\sin 2u$
20.  $\cos 2u$
21.  $\tan 2u$
22.  $\sin(x + 3\pi)$
23.  $\cos(\pi - x)$
24.  $\tan\left(x + \frac{\pi}{4}\right)$
25.  $\frac{\sin 2x}{2 \cos x}$
26.  $\tan 2x(1 + \tan x)$
27.  $\left(\frac{1 - \tan x}{2}\right) \tan 2x$

Answers:

- |                                   |                                    |                                    |                                     |
|-----------------------------------|------------------------------------|------------------------------------|-------------------------------------|
| 1. -240/161                       | 2. 119/169                         | 3. $\frac{-\sqrt{26}}{26}$         | 4. $\frac{\sqrt{15}}{8}$            |
| 5. $\frac{\sqrt{6}}{4}$           | 6. $-\sqrt{3}\sin x$               | 7. -2                              | 8. 3/5                              |
| 9. $\frac{-4\sqrt{3}+3}{10}$      | 10. 7/4                            | 11. $6 \sin 8x$                    | 12. $\frac{-\sqrt{2}+\sqrt{6}}{4}$  |
| 13. $\frac{\sqrt{2+\sqrt{3}}}{2}$ | 14. $\frac{-\sqrt{2}-\sqrt{6}}{4}$ | 15. $\frac{-\sqrt{2}-\sqrt{6}}{4}$ | 16. $\frac{\sqrt{26}}{26}$          |
| 17. $\frac{-5\sqrt{26}}{26}$      | 18. -1/5                           | 19. -120/169                       | 20. 119/169                         |
| 21. -120/119                      | 22. $-\sin x$                      | 23. $-\cos x$                      | 24. $\frac{\tan x + 1}{1 - \tan x}$ |
| 25. $\sin x$                      | 26. $\frac{2 \tan x}{1 - \tan x}$  | 27. $\frac{\tan x}{1 + \tan x}$    |                                     |