

AP Stats

$$\boxed{11.3-6, 10}$$

$$\boxed{11.3} \text{ SE} = 37/\sqrt{4} = 18.5$$

$$\boxed{11.4} \text{ a) } \begin{array}{c|c} \text{df} & \dots \text{ } \textcircled{.05} \\ \hline \textcircled{5} & \boxed{2.015} \end{array}$$

b) .99 left means .01 right

$$\boxed{2.518}$$

$$\boxed{11.5} \text{ a) } n-1=14 \quad \boxed{f^* = 2.145}$$

b) $n-1=19$.75 left \rightarrow .25 right

$$\boxed{f^* = 0.688}$$

$$\boxed{11.6} \text{ a) } n=10 \quad C=95\% \quad f^* \text{ for } 9 \text{ df} = \boxed{2.262}$$

$$\text{b) } n=20 \quad C=99\% \quad f^* \text{ for } 19 \text{ df} = \boxed{2.861}$$

$$\text{c) } n=7 \quad C=80\% \quad f^* \text{ for } 6 \text{ df} = \boxed{1.440}$$

$$\boxed{11.10} \text{ a) } n=6 \quad \bar{x} = 5.3667 \quad \text{SE}_{\bar{x}} = \frac{.66533}{\sqrt{6}} = \boxed{.2716}$$

df=5

$$\text{b) } 5.3667 \pm 2.015(.2716)$$

$$5.3667 \pm .5473$$

$$(4.8194, 5.9140)$$

We can be 90% confident that the patient's mean phosphate level is between 4.82 and 5.91 milligrams of phosphate per deciliter of blood.

AP Stats

$$\boxed{11.7, 9, 11-14}$$

$$\boxed{11.7} \quad H_0: \mu = 0 \quad n = 15 \quad t = 1.82$$

$$H_a: \mu > 0$$

$$a) \quad df = 15 - 1 = 14$$

$$b) \quad 1.761 \quad \rightarrow \quad 2.145$$

$$P \rightarrow \quad .05 \quad \quad .025$$

c) The p-value must be between .025 and .05

d) If $\alpha = .05$ $P < \alpha$. Yes, it is significant

If $\alpha = .01$ $P \not< \alpha$. No it is not significant

$$\boxed{11.9} \quad n = 4 \quad \bar{x} = \boxed{1.75} \quad SE_{\bar{x}} = \frac{.1291}{\sqrt{4}} = \boxed{.06455}$$

$$df = 3$$

$$b) \quad 90\% \quad t^* = 2.353 \quad 1.75 \pm 2.353(.06455)$$

$$1.75 \pm .1519$$

$$(1.598, 1.902)$$

$$\boxed{11.11} \quad H_0: \mu = 1.3 \quad \text{where } \mu \text{ is the mean absolutely}$$

$$H_a: \mu < 1.3 \quad \text{retractory period for poisoned rats}$$

$$n = 4 \quad df = 3 \quad t = \frac{1.75 - 1.3}{.06455} = 6.97$$

$$5.841 < t < 7.453$$

$$.005 > p\text{-value} > .0025$$

There is strong evidence against H_0 . ($p < .005$).

We conclude that DPT does slow nerve recovery.

11.12 a) μ is the mean difference between the yields for variety A and variety B

$$\mu = \mu_A - \mu_B$$

$$n = 10$$

$$\bar{x} = .34$$

$$s = .83$$

b) $H_0: \mu = 0$ where \uparrow

$H_a: \mu > 0$

$$c) t = \frac{.34 - 0}{.83/\sqrt{10}} = \boxed{1.295} \quad df = 9$$

$$P\text{-value} = .1137$$

There is not enough evidence to reject H_0 .

The observed difference could be due to chance.

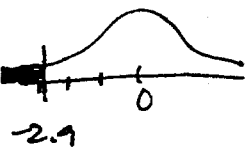
11.13 a) Randomly assign 12 or 13 people to group A (which will turn the right-hand knob first) and the rest to group B.

b) μ is the ^{mean} difference between right-handed times and left-handed times (for each right-handed person).

$H_0: \mu = 0$ ($\mu_R - \mu_L$) (in other words ...)

$H_a: \mu < 0$

$\mu_R = \mu_L \quad \mu_R < \mu_L$



$$c) \bar{x} = -13.32 \quad SE_{\bar{x}} = \frac{22.936}{\sqrt{25}} = 4.5872$$

$$t = \frac{-13.32 - 0}{22.936/\sqrt{25}} = \boxed{-2.9037}$$

$$df = 24 \quad p\text{-value} = \boxed{.0039}$$

Reject H_0

We conclude that there is a significant difference between right and left hand times. Right-hand times are less.

$$\boxed{11.14} \quad \bar{x} = -13.32 \quad 90\% t^* = 1.711$$

$$-13.32 \pm 1.711 \left(\frac{22.936}{\sqrt{25}} \right)$$

$$-13.32 \pm 7.849$$

$$(-21.169, -5.471)$$

There is a difference of between 5.5 and 21.2 seconds between right- and left hand times.

$$\bar{x}_R = 104.12 \quad \bar{x}_L = 117.44$$

What % of "left-hand times" is "right-hand times"?

$$\frac{x}{100} = \frac{104.12}{117.44} \quad 88.66\%$$

Right handed students working on right-handed threads would complete their task in about 89% of the time it would take them if they were working with left-handed threads.

AP Stats 11.16-18, 25, 26

11.16 $n = 200$ $H_0: \mu = 0$ where μ is the mean
 $\bar{x} = 332$ $H_a: \mu > 0$ increase in credit card charges
 $s = 108$

a) $t = \frac{332 - 0}{108/\sqrt{200}} = 43.5$ $p\text{-value} \approx 0$
Reject H_0

We have evidence to conclude that the mean increase in credit card charges is greater than zero.

b) $332 \pm t^* (108/\sqrt{200}) \Rightarrow (312.14, 351.86)$

c) We have an SRS and the sample size is large. We have no outliers so we meet the criteria for the t -test.

d) Make the offer to ^{an SRS of} 200 customers and choose another SRS of 200 as a control group. Compare the mean increase for the groups.

11.17 The distribution is slightly skewed right but there are no outliers.

$H_0: \mu = 224$ where μ is the mean dimension

$H_a: \mu \neq 224$ of the crankshafts.

$t = \frac{224.0019 - 224}{.0618/\sqrt{16}} = .1254$ $p = .9019$
fail to reject H_0

We do not have evidence to conclude that the dimension differs from 224.

$$\alpha = .05$$

11.18 $n = 12$

$H_0: \mu = 105$ where μ is the mean

$$\bar{x} = 104.13$$

$H_a: \mu \neq 105$ reading of all detectors

$$s = 9.397$$

$$t = \frac{104.13 - 105}{9.397 / \sqrt{12}} = -0.3195 \quad p = .7554$$

fail to reject H_0

9 | 2

9 | 5 7 8

10 | 0 2 4

10 | 5 5

11 | 1

11 | 9

12 | 2

There is not sufficient evidence to conclude that the detectors readings differ from 105.

11.25

a) SEM standard error of the mean

$$b) n = 3 \quad .01 = s / \sqrt{3} \quad \text{so } s = .01\sqrt{3} \approx .01732$$

$$c) 90\% t^* = 2.920 \quad df = 2$$

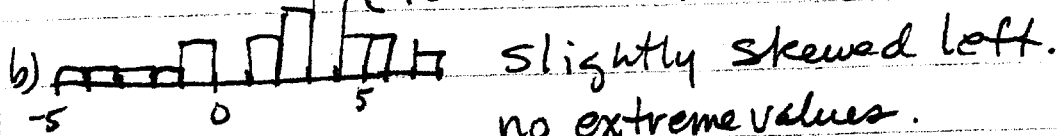
$$.84 \pm 2.920(.01) \Rightarrow (.8108, .8692)$$

11.26

a) $H_0: \mu = 0$ where μ is the mean increase in

$H_a: \mu > 0$ test scores for Spanish teachers.

(Post test - Pre test)



$$c) t = \frac{1.45 - 0}{3.2 / \sqrt{20}} = 2.0244 \quad p = .0286$$

Reject H_0 for $\alpha = .05$

Fail to reject H_0 for $\alpha = .01$

$$d) 1.45 \pm t^*(3.20 / \sqrt{20})$$

$$1.45 \pm 1.2385 \Rightarrow (.2115, 2.6885)$$

We are 90% confident that the mean increase in listening score was between .2115 and 2.6885.

11.31 a) two sample b) matched pair

11.32 a) single sample b) two sample

11.33 a) $H_0: \mu_1 = \mu_2$ where μ_1 is the beta-blocker

$\bar{x}_1 = 65.2$

$s_1 = 7.8$

$\bar{x}_2 = 70.3$

$s_2 = 8.3$

$H_a: \mu_1 < \mu_2$ mean pulse rate and μ_2 is the placebo mean pulse rate.

$t = -2.453$

$p = .0086$ $df = 57.8$ Reject H_0 at $\alpha = .05$ and $\alpha = .01$

We have evidence to conclude that beta-blockers do reduce the pulse rate.

b) $(-10.64, .439)$

11.34 $H_0: \mu_1 = \mu_2$ where μ_1 is the mean number of

$n_1 = 13$

$\bar{x}_1 = 3.47$

$s_1 = 1.21$

$\bar{x}_2 = 1.36$

$s_2 = .52$

$n_2 = 14$

$H_a: \mu_1 > \mu_2$ larvae in the control group and μ_2 is the mean # of larvae in the malathion group

$t = 5.809$

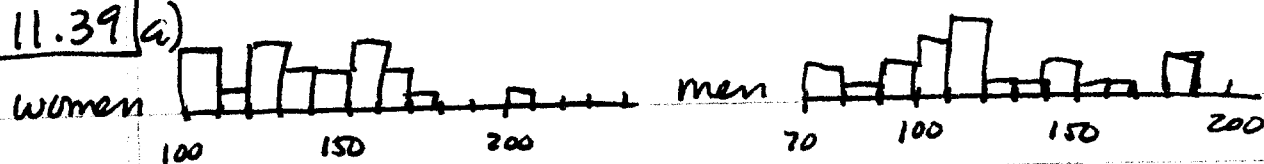
$p = .00001$ $df = 16$ Reject H_0 at $\alpha = .01$

We have evidence to conclude that malathion reduces the number of larvae on oats.

11.35 a) $t = 7.36$ if n is large the t -distribution can be approximated with the normal distribution. If $z = 7.36$ the p -value would be very small.

b) $df = 33 - 1 = 32$

11.39 a)



slightly skewed right

one possible outlier

slightly skewed right

two possible outliers

- b) $H_0: \mu_w = \mu_m$ where μ_w is the mean SSAT score for women and μ_m is the mean for men at this college.
 $H_a: \mu_w > \mu_m$

$$t = 2.056 \quad p = .0236$$

→ Since the sum of the sample sizes is almost 40 we may use the t -procedure (with some caution.)

We have evidence to conclude that the mean score for women is higher than for men.

c) for $\mu_w - \mu_m$ (3.5377, 36.073)

We are 90% confident that the mean difference between the scores for men and women is between 3.5 and 36.1 (with women scoring higher).

AP Stats 11.43 - 47

11.43 $n_1 = 10$ $\bar{x}_1 = 4.18$ $s_1 = .479$ skilled
 $n_2 = 8$ $\bar{x}_2 = 3.01$ $s_2 = .959$ unskilled

a) $H_0: \mu_1 = \mu_2$ where μ_1 is the mean velocity of
 $H_a: \mu_1 > \mu_2$ the knee for skilled rowers,
 μ_2 for unskilled rowers.

b) $t = 3.1583$ $p = .0052$ ($.0104/2$) $df = 7$
 Reject H_0 or 9.8

We have evidence to conclude that the mean
 knee velocity for skilled rowers is greater than
 that for novice rowers.

c) (.495, 1.845) using $df = 9.8$

11.44 $n_1 = 10$ $\bar{x}_1 = 70.37$ $s_1 = 6.10$ skilled
 $n_2 = 8$ $\bar{x}_2 = 68.45$ $s_2 = 9.04$ unskilled

$H_0: \mu_1 = \mu_2$ where μ_1 is the mean weight of
 $H_a: \mu_1 \neq \mu_2$ skilled rowers and μ_2 for unskilled.

$t = 0.5143$ $p = .6165$ fail to reject H_0

We do not have evidence to conclude that
 the weight of skilled rowers differs from
 the weight of novice rowers.

11.45 (27.915, 32.085)

We can say with 99% confidence that the mean difference between SAT scores for males and females is between 27.9 and 32.1. It is not necessary for the distribution to be normal because the sample size is very large.

11.46 $H_0: \mu_1 = \mu_2$ where μ_1 is the mean hemoglobin level of breast-fed infants and μ_2 for formula fed babies.
 $H_a: \mu_1 \neq \mu_2$
 $t = 1.654$ $p = .1065$ fail to reject H_0

We do not have evidence to conclude that the mean hemoglobin level of formula fed infants differs from breast-fed babies.

b) (-.2021, 2.0021)

c) We assume that both groups are SRSs and that both groups are normally distributed.

d) This is not an experiment. The mothers chose the feeding method. This may confound the conclusions by introducing other factors that affected the choice.

11.47 $H_0: \mu_1 = \mu_2$ where μ_1 is the ego strength
 $H_a: \mu_1 \neq \mu_2$ for the low-fitness group and
 μ_2 is for the high-fitness group.
 $t = -8.238$ $p = 3.909 \times 10^{-8} \approx 0$

Reject H_0 at $\alpha = .01$ or $.05$

We can conclude that there is a significant difference between the low- and high-fitness groups in the ego strength personality factor.

b) The subjects are all college professors and they all volunteered for a fitness program. There may be confounding factors in this study.

