

Two events are *dependent* if one event affects the other. Two events are *independent* if one event has no effect on the other.

Probability for B, dependent on A

If A and B are dependent, then $P(A \text{ and } B) = P(A) \cdot P(B|A)$.

If A and B are independent, then $P(A \text{ and } B) = P(A) \cdot P(B)$.

Example 1 There are 3 red markers, 4 blue markers, and 5 black markers in a box.

(a) Suppose you choose 2 markers at random, one at a time, with replacement.

Find the probability of choosing blue, then black.

$$P(\text{Blue \& Black}) = P(\text{Blue}) \times P(\text{Black})$$

$$= \frac{4}{12} \times \frac{5}{12} = \frac{1}{3} \times \frac{5}{12} = \frac{5}{36}$$

Independent

(b) Suppose you choose 3 markers at random, one at a time, without replacement.

Find the probability of choosing red, then blue, then blue.

$$P(R, B, B) = P(R) \cdot P(B) \cdot P(B)$$

$$= \frac{3}{12} \times \frac{4}{11} \times \frac{3}{10} = \frac{1}{4} \times \frac{4}{11} \times \frac{3}{10} = \frac{3}{110}$$

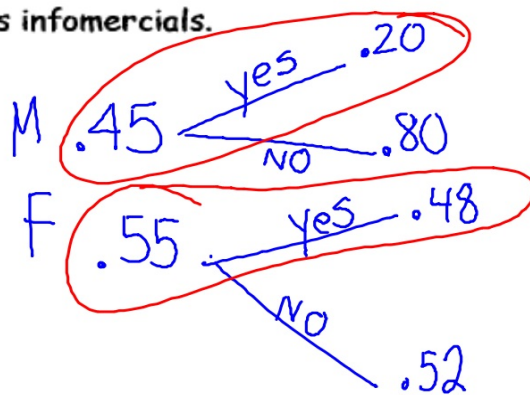
Dependent

$\frac{3}{110}$

Example 2 The probability of rain on a certain day is 10% in Placentia and 20% in Laguna Beach. Find the probability that it rains in at least one of the cities.

$$\begin{aligned}
 & P_{\text{not LB}} \text{ OR } \text{not } P \text{ \& } \text{LB} \text{ OR } P \text{ \& } \text{LB} \\
 & (\cancel{.10}) \times (\cancel{.80}) + (\cancel{.90}) \times (\cancel{.20}) + (\cancel{.10}) \times (\cancel{.20}) \\
 & .08 + .18 + .02 = .28 = 28\%
 \end{aligned}$$

Example 3 In a survey of adults 35-60 years old, 45% were males. Twenty percent of the males surveyed admitted they watched infomercials, and 48% of the females admitted watching infomercials. Use a tree diagram to find the probability that a randomly selected adult watches infomercials.



$$\begin{aligned}
 & M \text{ \& } \text{yes} \text{ OR } F \text{ \& } \text{yes} \\
 & (.45)(.20) + (.55)(.48) \\
 & + \\
 & = .354 = 35.4\%
 \end{aligned}$$