

8.6 Exponential Equations

std. 11.0

examples:

1 Solve: $16^{2x} = 64^{3x-2}$

$16 = 64^{1.6}$ $(4^2)^{2x} = (4^3)^{3x-2}$

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$$4x = 9x - 6$$

$$-5x = -6$$

$$x = \frac{6}{5}$$

1.2

2 Evaluate: $\log_4 15$

$$4^x = 15$$

$$\log_4 4^x = \log_4 15$$

$$x \log 4 = \log 15$$

$$x = \frac{\log 15}{\log 4} \approx 1.95$$

3 Solve: $8 + 6^{1.84} = 35$

$$8 + 6^{5x+4} = 35$$

$$6^{5x+4} = 27$$

$$\log 6^{5x+4} = \log 27$$

$$(5x+4) \log 6 = \log 27$$

$$5x+4 = \frac{\log 27}{\log 6}$$

$$-4.3 \approx x = \left(\frac{\log 27}{\log 6} - 4 \right) \div 5$$

$\bullet \ln e^x = x$

Proof: $\ln e^x = ?$

$$= \log_e e^x = ?$$

$$e^? = e^x \quad ? = x$$

4 Solve: $40e^{0.6x} = 240$

$$e^{0.6x} = 6$$

$$\ln e^{0.6x} = \ln 6$$

$$0.6x = \ln 6$$

$$2.99 \approx x = \frac{\ln 6}{0.6}$$