

# 9-5

## Percent

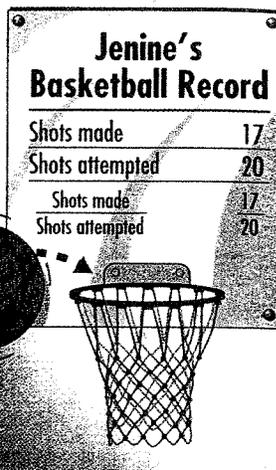
**Objective:** To write fractions and decimals as percents and to write percents as fractions and decimals.

### DATA ANALYSIS

Jenine attempted twenty shots during the last basketball game. The school paper reported that she made 85% of her shots.

The symbol % is read “percent.” A **percent** is a ratio that compares a number to 100. Percent means “per hundred,” “hundredths,” or “out of every hundred.”

$$1\% = \frac{1}{100} = 0.01$$



### Terms to Know

• *percent*

### Example 1

#### Solution

Write each fraction as a percent: a.  $\frac{17}{20}$       b.  $\frac{3}{8}$

a. Write  $\frac{17}{20}$  as a fraction whose denominator is 100.

$$\frac{17}{20} = \frac{17 \cdot 5}{20 \cdot 5} = \frac{85}{100} = 85\%$$

b. The denominator of  $\frac{3}{8}$  is not a factor of 100, so use division.

$$\frac{3}{8} = 0.37\frac{1}{2} \quad \leftarrow \text{Divide } 8 \overline{)3.00} \text{ to the } \textit{hundredths} \text{ place.}$$

$$= 37\frac{1}{2}\% \quad \leftarrow 0.37\frac{1}{2} \text{ means } 37\frac{1}{2} \textit{ hundredths.}$$

### Check Your Understanding

- When changing  $\frac{17}{20}$  to a percent in Example 1(a), why do you write the ratio as a fraction with a denominator of 100?
- If you used a calculator in Example 1(b), what number would be displayed for  $0.37\frac{1}{2}$ ?

Notice that to write a decimal as a percent, as in Example 1(b), you move the decimal point two places to the right and insert the symbol %.

$$0.37\frac{1}{2} = 37\frac{1}{2}\%$$

### Example 2

#### Solution

Write each decimal as a percent: a. 0.43      b. 0.09      c. 2.4

$$\begin{array}{lll} \text{a. } 0.43 = 0.43\% & \text{b. } 0.09 = 0.09\% & \text{c. } 2.4 = 2.40\% \\ & = 43\% & = 9\% & = 240\% \end{array}$$

You can also write percents as decimals and as fractions. To write a percent as a decimal, you move the decimal point two places to the left and drop the % symbol.

Notice in Examples 3 and 4 that a percent may be less than 1 or greater than 100.

### Example 3

Write each percent as a decimal.

- a. 74%      b. 0.25%      c. 110%      d.  $8\frac{1}{2}\%$

### Solution

- a.  $74\% = \underbrace{74}_{0.74}\% = 0.74$   
 b.  $0.25\% = \underbrace{0.25}_{0.0025}\% = 0.0025$   
 c.  $110\% = \underbrace{110}_{1.1}\% = 1.1$   
 d.  $8\frac{1}{2}\% = \underbrace{8.5}_{0.085}\% = 0.085$

### Example 4

Write each percent as a fraction or a mixed number in lowest terms.

- a. 125%      b. 3.6%      c.  $\frac{2}{5}\%$

### Solution

- a.  $125\% = \frac{125}{100} = \frac{5}{4} = 1\frac{1}{4}$   
 b.  $3.6\% = \frac{3.6}{100} = \frac{(3.6)(10)}{(100)(10)} = \frac{36}{1000} = \frac{9}{250}$   
 c.  $\frac{2}{5}\% = \frac{\frac{2}{5}}{100} = \frac{2}{5} \div 100 = \frac{2}{5} \cdot \frac{1}{100} = \frac{1}{250}$

### Check Your Understanding

- Describe how the position of the decimal point is changed in writing a percent as a decimal.
- In Example 3(d), why is  $8\frac{1}{2}$  rewritten as 8.5?
- Why are the numerator and denominator in Example 4(b) multiplied by 10?

## Guided Practice

### COMMUNICATION « Reading

- What is a percent?
- Describe two methods for changing a fraction to a percent.

Write each ratio as a percent.

- 18 out of 100
- 2:100
- 56 to 100
- $\frac{100}{100}$

7. To write  $1\frac{5}{8}$  as a percent, replace each  $\underline{\quad ? \quad}$  with the number that makes the statement true.

$$1 = \frac{?}{100} = \underline{\quad ? \quad} \%$$

$$\frac{5}{8} = 0.625 = \underline{\quad ? \quad} \%$$

$$1\frac{5}{8} = 1 + \frac{5}{8} = \underline{\quad ? \quad} \% + \underline{\quad ? \quad} \% = \underline{\quad ? \quad} \%$$

**Write each fraction or decimal as a percent.**

8.  $\frac{11}{50}$

9.  $\frac{3}{5}$

10.  $\frac{7}{8}$

11.  $\frac{1}{200}$

12. 0.45

13. 0.002

14. 1

15. 2.78

**Write each percent as a decimal.**

16. 65%

17. 4%

18. 9.2%

19.  $7\frac{1}{4}\%$

**Write each percent as a fraction or a mixed number in lowest terms.**

20. 36%

21. 0.5%

22.  $\frac{1}{4}\%$

23. 375%