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AP Calc BC

Final Review Part II

Let $f(x) = \begin{cases} x^2 - 2, & x < 1 \\ -\frac{1}{2}x + 1, & x \geq 1 \end{cases}$

Find

(a) $\lim_{x \rightarrow 1^-} f(x)$ (b) $\lim_{x \rightarrow 1^+} f(x)$ (c) $\lim_{x \rightarrow 1} f(x)$

16. Let $y = f(x)$ be the function shown at right. Which of the following statements is false?

- (A) $\lim_{x \rightarrow 1} f(x) = 1$
(B) $\lim_{x \rightarrow 2^-} f(x) = 2$
(C) $\lim_{x \rightarrow 0^+} f(x) = \lim_{x \rightarrow 0^-} f(x)$
(D) $\lim_{x \rightarrow -1} f(x) = 2$
(E) $\lim_{x \rightarrow -1^+} f(x) = 2$

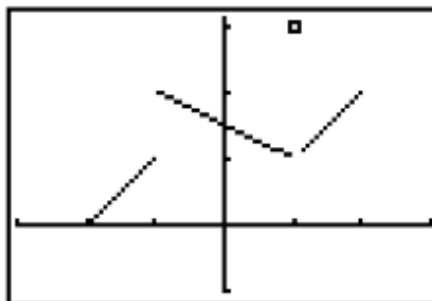


Figure 16

17. The graph of function f is shown at right. At which of the following points is f continuous?

- (A) $x = -3$
(B) $x = -1$
(C) $x = 1$
(D) $x = 3$
(E) all of the above

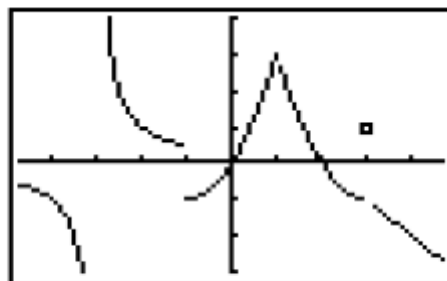


Figure 17

1998 AB 4

Let f be a function with $f(1) = 4$ such that for all points (x, y) on the graph of f the slope is

given by $\frac{3x^2 + 1}{2y}$

- (a) Find the slope of the graph of f at the point where $x = 1$
(b) Write an equation for the line tangent to the graph of f at $x = 1$ and use it to approximate $f(1.2)$

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1992 AB4

Consider the curve defined by $y + \cos y = x + 1$ $0 \leq y \leq 2\pi$ for

- (a) Find $\frac{dy}{dx}$ in terms of y .
- (b) Write an equation for each vertical tangent to the curve.
- (c) Find $\frac{d^2y}{dx^2}$ in terms of y .
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- 6) Given: $f(x) = x^3 - 5x^2 + 3x + 6$. Find the coordinates of all relative extrema. Find the x-coordinates of any points of inflection. Sketch the graph.
- 7) Given: $y = x^4 - 4x^3$. Find the coordinates of all relative maxima and minima and points of inflection. Discuss the concavity. Find the roots of the function. Sketch the graph.
- 8) A particle moves along the x-axis according to the law $s = 2t^3 - 9t^2 + 12t - 4$.
- a) For what values of t is s increasing?
- b) For what values of t is the velocity increasing?
- c) Find the velocity when $t = 3/2$.
- d) Find the acceleration when $t = 2$.
9. Let $f(x) = 12x^{2/3} - 4x$. (No calculator)
- a) Find the coordinates for all critical points.
- b) Determine whether the critical points found in part a) are extrema. Justify your answer.
- c) Find the coordinates of all points of inflection.
- d) For what values of x is f concave up.
- e) Sketch the graph of f .

1. Let f be the function defined by $f(x) = (1 + \tan x)^{3/2}$ for $-\frac{\pi}{4} < x < \frac{\pi}{2}$
- a. Write an equation for the line tangent to the graph of f at the point where $x=0$
- b. Using the equation found in part (a), approximate $f(0.02)$

2001 AB6

1. The function f is differentiable for all real numbers. The point $(3, \frac{1}{4})$ is on the graph of $y=f(x)$, and the slope at each point (x,y) is given by $\frac{dy}{dx} = y^2(6 - 2x)$

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- a. Find $\frac{d^2y}{dx^2}$ and evaluate it at the point $(3, \frac{1}{4})$

1997 AB4

1. Let f be the function given by $f(x) = x^3 - 6x^2 + 2$, where p is an arbitrary constant.
- Write an expression for $f'(x)$ and use it to find the relative maximum and minimum values. Show the analysis that lead to our conclusion.
 - Determine the concavity of the graph. Justify your answer
 - Sketch the graph of f , f' and f''

2001 AB4

1. Let h be a function defined for all $x \neq 0$ such that $h(4) = -3$ and the derivative of h is given by $h'(x) = \frac{x^2 - 2}{x}, x \neq 0$
- Find all values of x for which the graph of h has a horizontal tangent and determine whether h has a local maximum, a local minimum, or neither at each of these values. Justify your answer.
 - On what intervals, if any, is the graph of h concave up? Justify your answer.
 - Write an equation for the line tangent to the graph of h at $x = 4$
 - Does the line tangent to the graph of h at $x = 4$ lie above or below the graph of h for $x > 4$? Why?

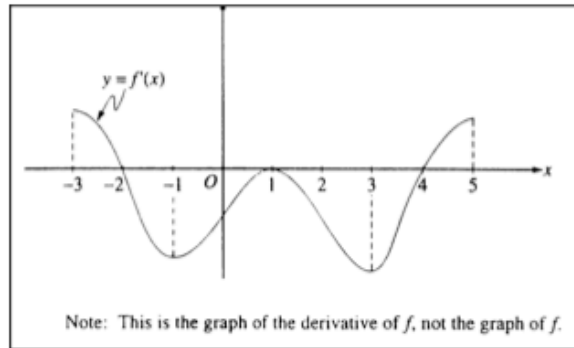
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1996 AB1

The figure below shows the graph of f' , the derivative of f . The domain is the set of all real values of x such that $-3 \leq x \leq 5$.



96 AB1

- For what values of x does f have a relative maximum? Why?
- For what values of x does f have a relative minimum? Why?
- On what intervals is the graph of f concave upward? Use f' to justify your answer.
- Suppose that $f(1) = 0$. Draw a sketch that shows the general shape of the graph of the function f on the open interval $0 < x < 2$.

- A balloon is rising vertically over a point A at the rate of 15ft/sec. A point B on the ground is level with point A and is 30 ft. from A. At what rate is the distance between B and the balloon changing when the balloon is 40 ft high?

1990 AB4

The radius r of a sphere is increasing at a constant rate of 0.04 cm/s (The volume of a sphere is given by $V = \frac{4}{3}\pi r^3$)

- At the time when radius of the sphere is 10 cm, what is the rate of the increase of its volume?
- At the time when the volume and the radius of the sphere are increasing at the same numerical rate, what is the radius?

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1. Let R be the region enclosed between the graph of $y = -\frac{1}{2}x^2 + 3x - \frac{5}{2}$ and the x -axis on the closed interval $[1, 5]$.



$[0, 6]$ by $[-3, 3]$

Use the Midpoint Rectangular Approximation method with four rectangles of equal width to estimate the area. Sketch the graph and the rectangles. Indicate coordinates. Show your steps.

8) $f(x) = \ln(x^{3/2} + 2x^{3/5} - 4x^{4/7})$

9) $f(x) = \frac{1}{\sqrt[4]{x^2 + 2x + 3}}$

10) $g(x) = \sqrt[3]{\frac{3x+4}{2x+3}}$

11) $F(x) = \arctan(4x + 3)$

12) $f(x) = \sin^3(3x^2) e^{-4x}$

13) $f(x) = \cot 3x \sec^4 2x$

14) $\sin(\tan(2x + 1))$