

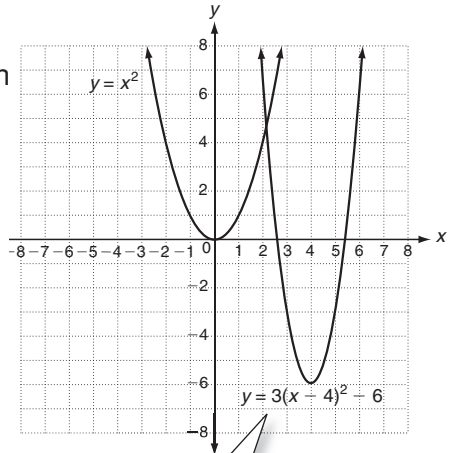
Date \_\_\_\_\_

Dear Family,

In Chapter 5, your child will graph quadratic functions, solve quadratic equations and inequalities, and learn to operate with complex numbers.

A **quadratic function** is one in which the variable is squared. The parent quadratic function is  $f(x) = x^2$ , which forms as a U-shaped **parabola** with **vertex**  $(0, 0)$ .

The parent function can be transformed to form a variety of parabolas. **Vertex form** helps you identify transformations.



**vertex form:**  $f(x) = a(x - h)^2 + k$

$a$  indicates a reflection across the  $x$ -axis and/or a vertical stretch or compression.

$h$  indicates a horizontal translation.

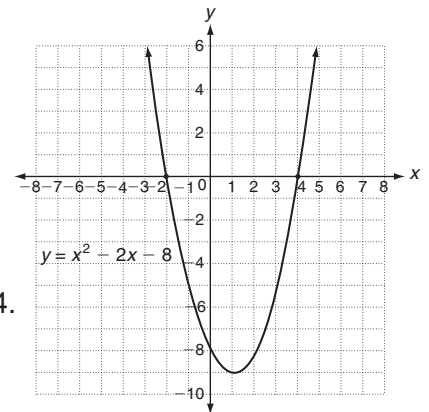
$k$  indicates a vertical translation.

$y = 3(x - 4)^2 - 6$  was stretched vertically by a factor of 3, and the vertex is translated to  $(4, -6)$ .

A quadratic function may also be in **standard form**, which helps identify other properties of the parabola, such as the  $y$ -intercept (the coefficient  $c$ ).

**standard form:**  $f(x) = ax^2 + bx + c$

The  $x$ -intercepts of a parabola are input values of  $x$  that make the output of  $f(x) = ax^2 + bx + c$  equal to zero. Hence, the  $x$ -intercepts are also called **zeros**. You can find the zeros of a function by graphing it.



**quadratic function:**  $f(x) = x^2 - 2x - 8$

From the graph, the zeros are  $x = -2$  and  $x = 4$ .

Closely related to a quadratic function is the quadratic equation  $ax^2 + bx + c = 0$ . The solutions to a quadratic equation are called **roots**. You can find roots by factoring and using the **Zero Product Property**. The roots are equivalent to the zeros.

**quadratic equation:**  $x^2 - 2x - 8 = 0$

$(x + 2)(x - 4) = 0$

$x + 2 = 0$  or  $x - 4 = 0$

$x = -2$  or  $x = 4$

**Zero Product Property**

If two quantities multiply to zero, then at least one is zero.

Many quadratic expressions are **trinomials** (contain three terms) that factor into two **binomials** (contain two terms). If the two binomial factors are identical, the original expression is called a **perfect-square trinomial**.

$$\underbrace{x^2 - 10x + 25}_{\text{perfect-square trinomial}} = (x - 5)(x - 5) = (x - 5)^2$$

**Completing the square** is a method of solving a quadratic equation by making a perfect-square trinomial. Then you use a square root to solve.

**Solve  $x^2 + 6x = 1$ .**

$$x^2 + 6x + \textcircled{9} = 1 + \textcircled{9}$$

*9 makes  $x^2 + 6x$  a perfect-square.*

$$(x + 3)^2 = 10$$

*Factor the left side.*

$$x + 3 = \pm\sqrt{10}$$

*Take the square root of both sides.*

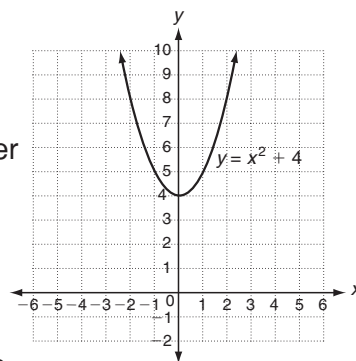
$$x = -3 \pm\sqrt{10}$$

*Solve for  $x$ .*

If you complete the square for the general equation  $ax^2 + bx + c = 0$ , you get the **Quadratic Formula**:

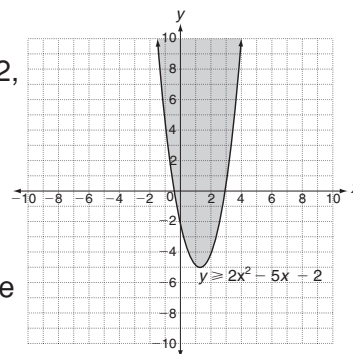
$$\text{If } ax^2 + bx + c = 0, \text{ then the solutions are } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$

Some quadratic functions, such as  $f(x) = x^2 + 4$ , have no  $x$ -intercepts. Likewise, the equation  $0 = x^2 + 4$  has no *real* roots because you get  $x = \pm\sqrt{-4}$ . The square root of a negative number is called an **imaginary number**, and the **imaginary unit** is  $i = \sqrt{-1}$ . So,  $0 = x^2 + 4$  does have two *imaginary* roots,  $x = \pm 2i$ .



A **complex number** is one that can be written in the form  $a + bi$ . For example, in  $7 - 2i$ , the **real part** is 7 and the **imaginary part** is  $-2i$ . Complex numbers can be graphed in the **complex plane** (which has a real axis and an imaginary axis), and they can be added, subtracted, multiplied, divided, or raised to powers.

**Quadratic inequalities** in *two* variables, such as  $y \geq 2x^2 - 5x - 2$ , are graphed similar to linear inequalities in two variables: solid or dashed boundary line with shading above or below. Quadratic inequalities in *one* variable are graphed on a number line.



Quadratic equations have many real-world applications, such as the height of a *projectile* (an object that is thrown or launched) as gravity acts on it over time. If the data isn't perfectly quadratic, you might use **regression** to find a best-fit **quadratic model**.

For additional resources, visit [go.hrw.com](http://go.hrw.com) and enter the keyword MB7 Parent.