

You must do your work on a separate piece of paper.

Solve # 1 – 6 .

1.  $\sin 2x = \sin x; 0 \leq x < 2\pi$

2.  $\tan 2x + \tan x = 0; 0 \leq x < 2\pi$

3.  $3 \sin x = 1 + \cos 2x; 0 \leq x < 2\pi$

4.  $4 \sin x \cos x = \sqrt{3}; 0 \leq x < 360^\circ$

5.  $\cos 8x \cos 5x + \sin 8x \sin 5x = -1; 0 \leq x < 360^\circ$

6.  $\sin 2x \tan x = 1; 0 \leq x < 360^\circ$

7.  $\sin x \cos x = \frac{1}{2}; 0 \leq x < 2\pi$

8.  $2 \cos(x + 45^\circ) = 1; 0^\circ \leq x < 360^\circ$

9. Given:  $\tan \theta = \frac{5}{12}, \theta$  in Q III.

Find: a)  $\tan 2\theta$       b)  $\sin 2\theta$       c)  $\cos \frac{1}{2} \theta$

10. Expand and simplify:  $\csc(180^\circ - \theta)$

11. Find  $\tan(\alpha + \beta)$  given  $\sin \alpha = \frac{3}{5}, \alpha$  in Q I and  $\cos \beta = \frac{5}{13}, \beta$  in Q IV

12. Show:  $\cos(\alpha - \beta) - \cos(\alpha + \beta) = 2 \sin \alpha \sin \beta$

13. Show:  $\sin(\alpha + \beta) - \sin(\alpha - \beta) = 2 \sin \beta \cos \alpha$

Find the EXACT VALUE of each of the following.

14.  $\sin 15^\circ \cos 15^\circ$

15.  $\sin 112.5^\circ$

$\cos \theta = \frac{-4}{5}; 90^\circ < \theta < 180^\circ$ . Find the following:

16.  $\sin 2\theta$

17.  $\cos 2\theta$

18.  $\cos\left(\frac{\theta}{2}\right)$

19.  $\sin\left(\frac{\theta}{2}\right)$

20.  $\tan\left(\frac{\theta}{2}\right)$

Answers:

1)  $0, \frac{\pi}{3}, \frac{5\pi}{3}, \pi$

2)  $0, \frac{\pi}{3}, \frac{2\pi}{3}, \pi, \frac{4\pi}{3}, \frac{5\pi}{3}$

3)  $\frac{\pi}{6}, \frac{5\pi}{6}$

4)  $30^\circ, 60^\circ, 210^\circ, 240^\circ$

5)  $60^\circ, 180^\circ, 300^\circ$

6)  $45^\circ, 135^\circ, 225^\circ, 315^\circ$

7)  $\frac{\pi}{4}, \frac{5\pi}{4}$

8)  $15^\circ; 255^\circ$

9)  $\frac{120}{119}, \frac{120}{169}, \frac{-\sqrt{26}}{26}$

10)  $\csc \theta$

11)  $\frac{-33}{56}$

14.  $\frac{1}{4}$

15.  $\frac{\sqrt{2+\sqrt{2}}}{2}$

16.  $-24/25$

17.  $7/25$

18.  $\frac{\sqrt{10}}{10}$

19.  $\frac{3\sqrt{10}}{10}$

20. 3