

**Translations and Reflections**

$y = a \sin b(x-h) + k$

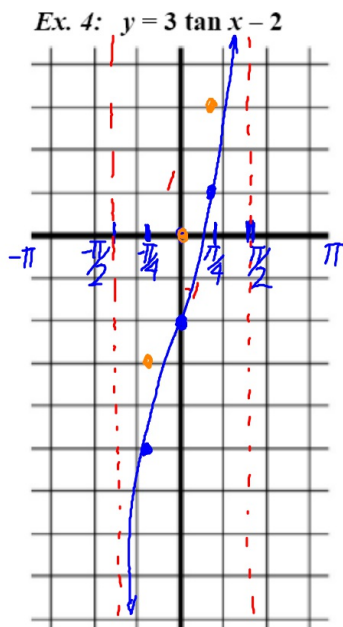
$y = a \cos b(x-h) + k$

$y = a \tan b(x-h) + k$

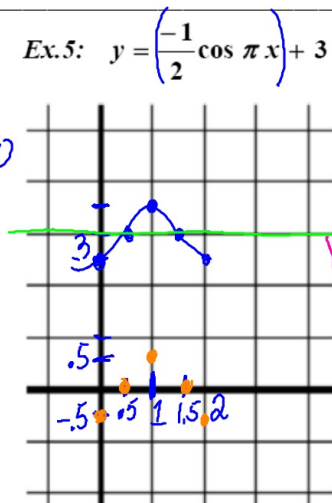
$h$ : horizontal translation (phase shift)

$k$ : vertical translation

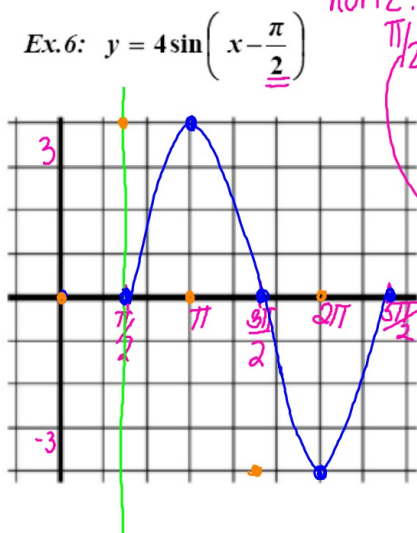
if  $a < 0$ : reflection across line  $y = k$



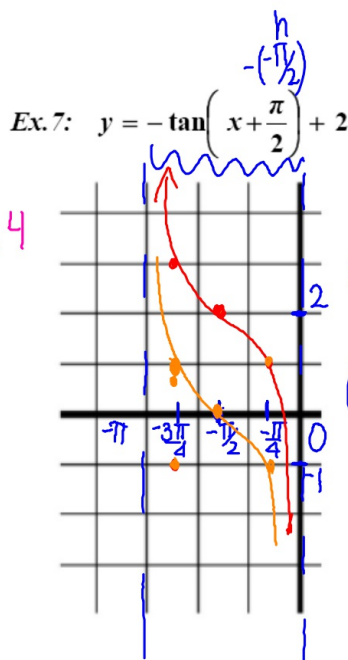
down 2  
 $Fa = F3$   
 $-\infty < y < \infty$   
 per =  $\pi$



up 3  
 period 2  
 amp  $\frac{1}{2}$   
 reflection  
 across  
 $y = 3$



horiz. trans.  
 $\frac{\pi}{2}$  (right)  
 amp = 4  
 $-4 \leq y \leq 4$   
 per =  $2\pi$   
 $\frac{\pi}{2} + \frac{2\pi}{2} = \frac{5\pi}{2}$



up 2  
 left  $\frac{\pi}{2}$   
 reflection  
 across  $y = 2$   
 period  $\pi$

