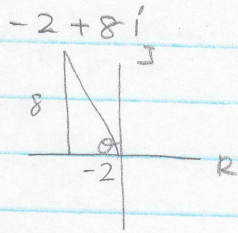


Chapter 11 Review C

1

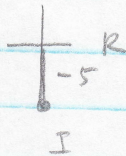


$$r = \sqrt{4+64} = 2\sqrt{17}$$

$$\theta = 180^\circ - \tan^{-1}\left(\frac{8}{2}\right) = 180^\circ - 76.0^\circ = 104.0^\circ$$

$$-2 + 8i = 2\sqrt{17} \operatorname{cis} 104.0^\circ$$

2



$$r = 5 \quad ; \quad \theta = \frac{3\pi}{2}$$

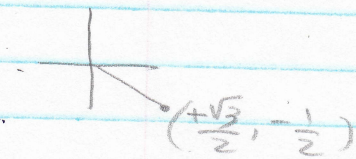
$$0 - 5i = 5 \operatorname{cis} \frac{3\pi}{2}$$

3

$$18 \operatorname{cis} 330^\circ = 18 (\cos 330^\circ + i \sin 330^\circ)$$

$$= 18 \left(\frac{\sqrt{3}}{2}\right) + i (18) \left(-\frac{1}{2}\right)$$

$$18 \operatorname{cis} 330^\circ = 9\sqrt{3} - 9i$$



4

$$18 \operatorname{cis} 201^\circ = 18 (\cos 201^\circ + i \sin 201^\circ)$$

$$= 18 (-16.8 - 6.5i) \quad (\text{use calc})$$

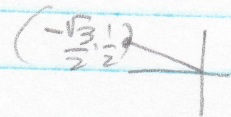
5

$$(9 \operatorname{cis} 60^\circ) (8 \operatorname{cis} 90^\circ) =$$

$$72 \operatorname{cis} (60^\circ + 90^\circ) = 72 \operatorname{cis} 150^\circ$$

$$72 (\cos 150^\circ + i \sin 150^\circ) = 72 \left(-\frac{\sqrt{3}}{2}\right) + i (72) \left(\frac{1}{2}\right)$$

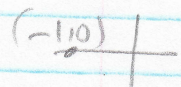
$$= -36\sqrt{3} + 36i$$



$$(9 \operatorname{cis} 60^\circ)^3 = 9^3 \operatorname{cis} 3(60^\circ) = 729 \operatorname{cis} 180^\circ$$

$$= 729 (\cos 180^\circ + i \sin 180^\circ)$$

$$= 729(-1) + i(729)(0) = -729 + 0i$$



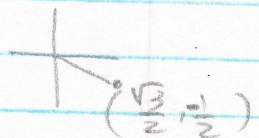
$$\frac{9 \operatorname{cis} 60^\circ}{8 \operatorname{cis} 90^\circ}$$

$$= \frac{9}{8} \operatorname{cis} (60^\circ - 90^\circ) = \frac{9}{8} \operatorname{cis} (-30^\circ) = \frac{9}{8} \operatorname{cis} (-30^\circ + 360^\circ)$$

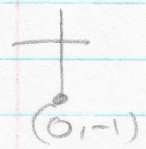
$$= \frac{9}{8} \operatorname{cis} 330^\circ$$

$$= \frac{9}{8} (\cos 330^\circ + i \sin 330^\circ) = \frac{9}{8} \left(\frac{\sqrt{3}}{2}\right) + i \left(\frac{9}{8}\right) \left(-\frac{1}{2}\right)$$

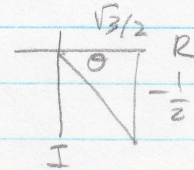
$$= \frac{9\sqrt{3}}{16} - \frac{9}{16}i$$



6. $(2 \operatorname{cis} \frac{5\pi}{6})^{-3} = 2^{-3} \operatorname{cis} \left[-3 \left(\frac{5\pi}{6} \right) \right]$
 $= \frac{1}{8} \operatorname{cis} \left(-\frac{5\pi}{2} \right) = \frac{1}{8} \operatorname{cis} \left(-\frac{5\pi}{2} + 2 \cdot 2\pi \right) = \frac{1}{8} \operatorname{cis} \left(-\frac{5\pi}{2} + \frac{8\pi}{2} \right)$
 $= \frac{1}{8} \operatorname{cis} \frac{3\pi}{2} = \frac{1}{8} \left(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2} \right)$
 $= \frac{1}{8} (0) + i \left(\frac{1}{8} \right) (-1) = 0 - \frac{1}{8} i$

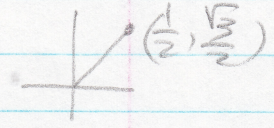


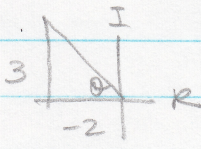
7. $\left(\frac{\sqrt{3}}{2} - \frac{1}{2} i \right)^{10}$



$r = \sqrt{\frac{3}{4} + \frac{1}{4}} = 1$
 $\theta = 360^\circ - \tan^{-1} \left(\frac{1/2}{\sqrt{3}/2} \right) = 360^\circ - \tan^{-1} \left(\frac{1}{\sqrt{3}} \right) = 360^\circ - 30^\circ = 330^\circ$

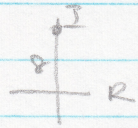
$(1 \operatorname{cis} 330^\circ)^{10} = 1^{10} \operatorname{cis} 10 \cdot 330^\circ = 1 \operatorname{cis} 3300^\circ$
 $= 1 \operatorname{cis} (3300^\circ - 9 \cdot 360^\circ) = 1 \operatorname{cis} 60^\circ$
 $= \cos 60^\circ + i \sin 60^\circ$
 $= \frac{1}{2} + \frac{\sqrt{3}}{2} i$



8.  $r = \sqrt{4+9} = \sqrt{13}$
 $\theta = 180^\circ - \tan^{-1} \left(\frac{3}{2} \right)$
 $\theta = 123.6900675 \dots$ (keep in calc)

$(\sqrt{13} \operatorname{cis} 123.6900675 \dots)^6 = 2197 \operatorname{cis} 742.1404052 \dots$ (keep in calc)
 $= 2197 (\cos 742.1404052 \dots + i \sin 742.1404052 \dots)$
 $2035 + 828i$

9. cube root $8i$



$r = 8$; $\theta = 90^\circ + n \cdot 360^\circ$
 $8i = 8 \operatorname{cis} (90^\circ + n \cdot 360^\circ)$
 cube root of $8i = (8 \operatorname{cis} (90^\circ + n \cdot 360^\circ))^{\frac{1}{3}}$
 $= 8^{\frac{1}{3}} \operatorname{cis} \frac{1}{3} (90^\circ + n \cdot 360^\circ)$
 $r = 2 \operatorname{cis} 30^\circ + n \cdot 120^\circ$

$$\begin{aligned}
 n=0 \quad 2 \cos 30^\circ &= 2(\cos 30^\circ + i \sin 30^\circ) & \left(-\frac{\sqrt{3}}{2}, \frac{1}{2}\right) & \begin{array}{c} \nearrow \\ \searrow \end{array} & \left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right) \\
 & 2\left(\frac{\sqrt{3}}{2}\right) + i(2)\left(\frac{1}{2}\right) = \sqrt{3} + i \\
 n=1 \quad 2 \cos 30^\circ + 120^\circ &= 2 \cos 150^\circ & & & \\
 & 2\left(-\frac{\sqrt{3}}{2}\right) + i(2)\left(\frac{1}{2}\right) = -\sqrt{3} + i & & \uparrow & \\
 n=2 \quad 2 \cos 30^\circ + 240^\circ &= 2 \cos 270^\circ & & & \downarrow \\
 & 2(0) + i(2)(-1) = 0 - 2i & & & (0, -1)
 \end{aligned}$$

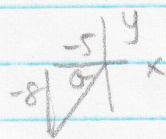
$$\begin{aligned}
 (10) \quad -\sqrt{2} + i\sqrt{2} & \begin{array}{c} \text{P} \\ \nearrow \\ \sqrt{2} \\ \text{R} \\ \searrow \\ -\sqrt{2} \end{array} & r = \sqrt{2+2} = 2 & \theta = 180^\circ - \tan^{-1}\left(\frac{\sqrt{2}}{\sqrt{2}}\right) = \\
 & & & 135^\circ + n \cdot 360^\circ
 \end{aligned}$$

$$\begin{aligned}
 -\sqrt{2} + i\sqrt{2} &= 2 \cos(135^\circ + n \cdot 360^\circ) \\
 \text{square roots of } (-\sqrt{2} + i\sqrt{2}) &= [2 \cos(135^\circ + n \cdot 360^\circ)]^{\frac{1}{2}} \\
 &= 2^{\frac{1}{2}} \cos \frac{1}{2}(135^\circ + n \cdot 360^\circ) \\
 &= \sqrt{2} \cos 67.5^\circ + n \cdot 180^\circ
 \end{aligned}$$

$$\begin{aligned}
 n=0 \rightarrow \sqrt{2} \cos 67.5^\circ &= \sqrt{2}(\cos 67.5^\circ + i \sin 67.5^\circ) \\
 &= 0.54 + 1.31i
 \end{aligned}$$

$$\begin{aligned}
 n=1 \rightarrow \sqrt{2} \cos(67.5^\circ + 180^\circ) &= \sqrt{2} \cos 247.5^\circ = \sqrt{2}(\cos 247.5^\circ + i \sin 247.5^\circ) \\
 &= -0.54 - 1.31i
 \end{aligned}$$

$$11 \quad (-5, -8)$$



$$r = \sqrt{25+64} = \sqrt{89}$$

$$\theta = 180^\circ + \tan^{-1}\left(\frac{8}{5}\right) = 238.0^\circ$$

$$(-5, -8) = (\sqrt{89}, 238.0^\circ)$$

no i

no cis

$$12 \quad \left(18, \frac{2\pi}{3}\right) = 18 \angle$$

$$x = 18 \cos \frac{2\pi}{3} = 18\left(-\frac{1}{2}\right) = -9$$

$$y = 18 \sin \frac{2\pi}{3} = 18\left(\frac{\sqrt{3}}{2}\right) = 9\sqrt{3}$$

$$\left(18, \frac{2\pi}{3}\right) = (-9, 9\sqrt{3})$$

no cis

no i

$$13 \quad r = 1 + 4 \sin \theta$$

θ	$4 \sin \theta$	$1 + 4 \sin \theta$
0°	0	1
30°	0.5	3
90°	1	5
150°	0.5	3
180°	0	1
210°	-0.5	-1
270°	-1	-3
330°	-0.5	-1
360°	0	1

