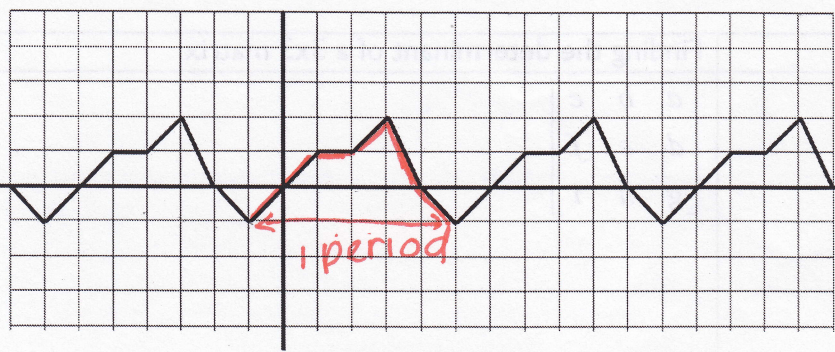


1. Given $y = f(x)$



Find:

a) period 6

c) $f(45) = f(3) = 2$

b) amplitude $\frac{1}{2}$

d) $f(-70) = f(-4) = 1$

$6 \overline{) 45} = 7 \text{ R } 3$
 $6 \overline{) 70} = 11 \text{ R } 4$

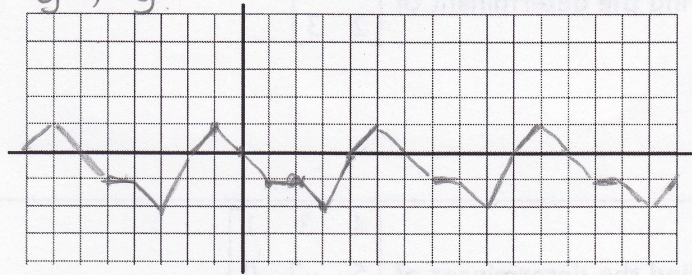
$\frac{2 - (-1)}{2} = \frac{3}{2}$

-1	0	1	2	3	4	5
-1	0	1	1	2	0	-1

2. $y = -f(x)$

$y \rightarrow -y$

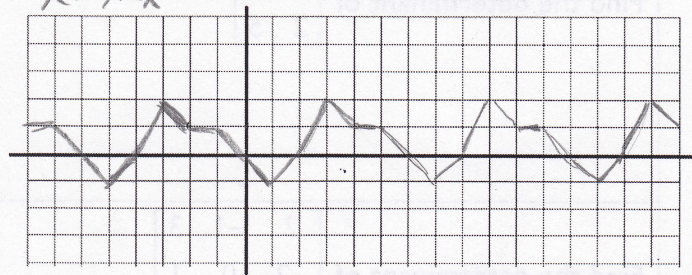
-1	0	1	2	3	4	5
1	0	-1	-1	-2	0	1



3. $y = f(-x)$

$x \rightarrow -x$

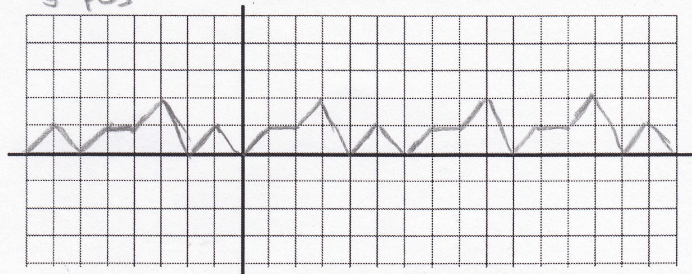
1	0	-1	-2	-3	-4	-5
-1	0	1	1	2	0	-1



4. $y = |f(x)|$

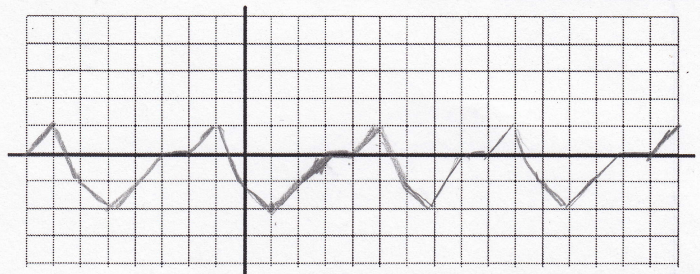
y pos

-1	0	1	2	3	4	5
1	0	1	1	2	0	1



5. $y + 1 = f(x - 2)$

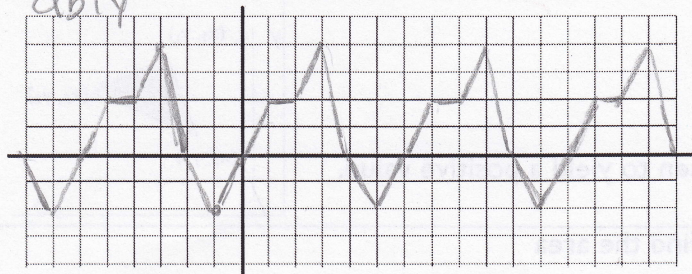
1	2	3	4	5	6	7
-2	-1	0	0	1	-1	-2



6. $y = 2f(x)$

dble y

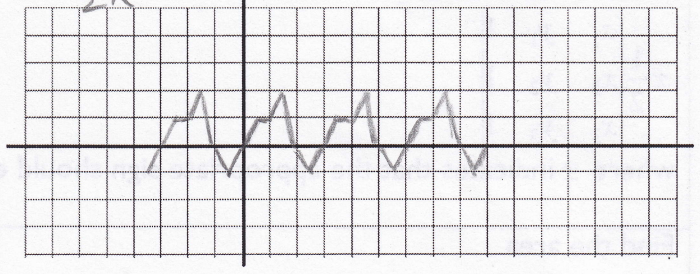
-1	0	1	2	3	4	5
-2	0	2	2	4	0	-2



7. $y = f(2x)$

$\frac{1}{2}x$

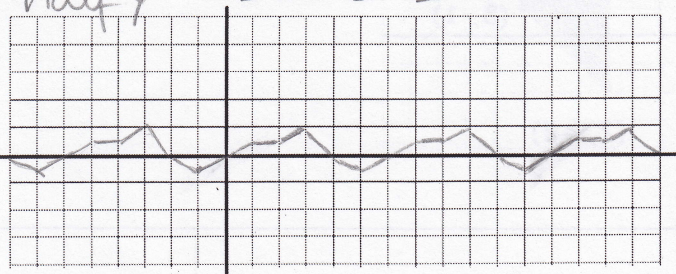
$-\frac{1}{2}$	0	$\frac{1}{2}$	1	$\frac{3}{2}$	2	$\frac{5}{2}$
-1	0	1	1	2	0	-1



8. $y = \frac{1}{2}f(x)$

half y

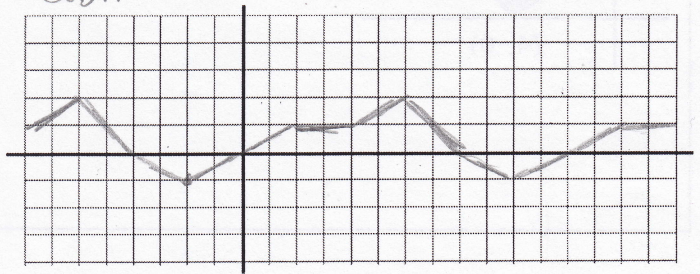
-1	0	1	2	3	4	5
$-\frac{1}{2}$	0	$\frac{1}{2}$	$\frac{1}{2}$	1	0	$-\frac{1}{2}$



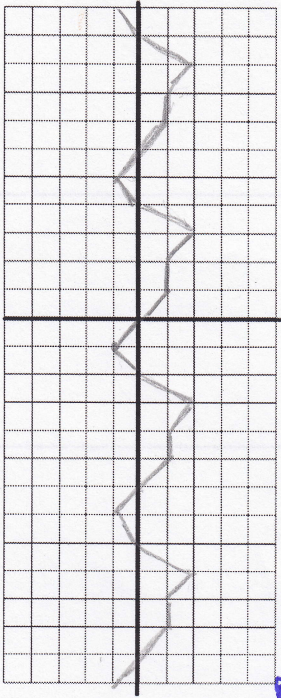
9. $y = f\left(\frac{1}{2}x\right)$

dble x

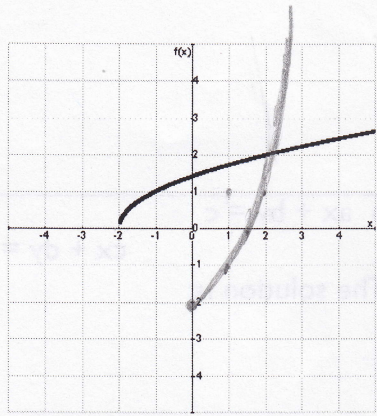
-2	0	2	4	6	8	10
-1	0	1	1	2	0	-1



10) x and y switched

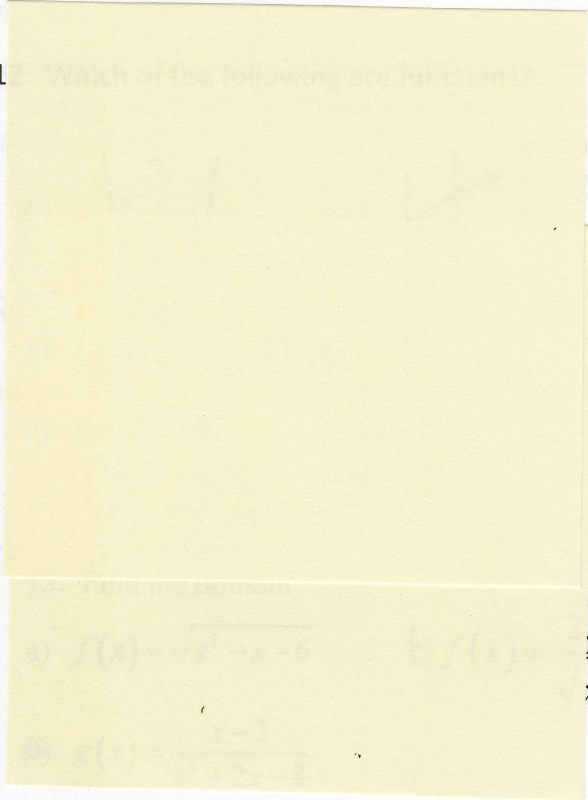


11. Graph $y = f^{-1}(x)$



-2	-1	0	2	↕	switch
0	1	1.5	1	↕	

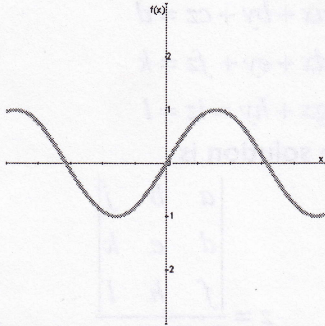
-1	0	1	1	2	0	-1
-1	0	1	2	3	4	5



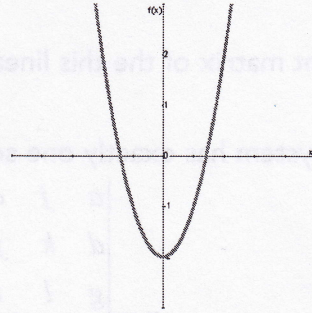
14. Find the range:

a) $y = |x|$

b)

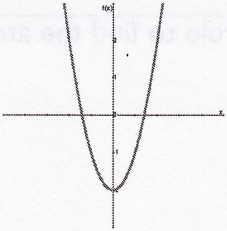


c)

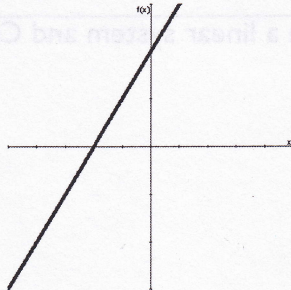


15) Which of the following have an inverse function?

a)

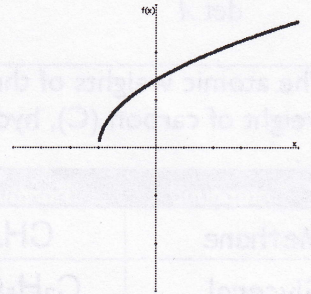


b)



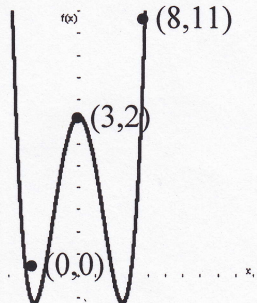
c) $y = |x| + 3$

d)

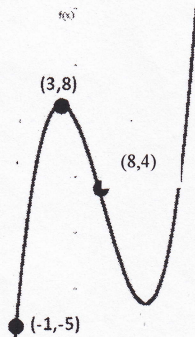


16) Name as many other points on graph as possible using point and line symmetry.

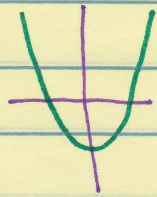
a)



b)



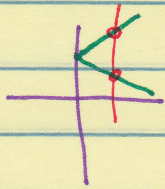
12.



Function

passes Vertical Line Test

b



not a function

Doesn't pass VLT

c

$$x + y^2 = 16$$

$$x = 7 \rightarrow 7 + y^2 = 16$$

$$y^2 = 9$$

$$y = \pm 3$$

There are 2 values of y for $x=7 \rightarrow$ not a function

d.

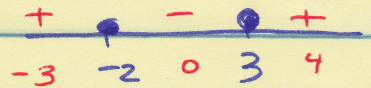
$xy=4 \rightarrow y = \frac{4}{x}$ yes. For every x , there's only 1 y value.

13

$$\sqrt{x^2 - x - 6}$$

$$: x^2 - x - 6 > 0$$

$$(x-3)(x+2) > 0$$



$$4: ++ \rightarrow (+)$$

$$0: -+ \rightarrow (-)$$

$$-3: -- \rightarrow (+)$$

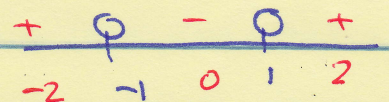
$$x > 3 \text{ or } x < -2$$

b.

$$\frac{2x-3}{\sqrt{x^2-1}}$$

$x^2 - 1 > 0$ can't be zero because denominator $\neq 0$

$$(x+1)(x-1) > 0$$



$$2: ++ \rightarrow (+)$$

$$0: +- \rightarrow (-)$$

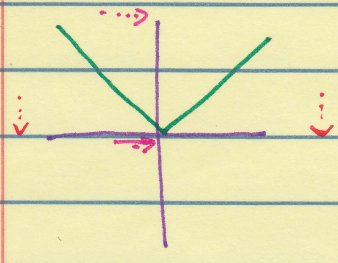
$$-2: -- \rightarrow (+)$$

$$x > 1 \text{ or } x < -1$$

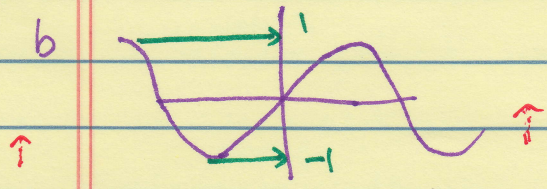
c. $\frac{x-3}{x^2+2x-8}$

$x^2+2x-8 \neq 0$ can't divide by zero
 $(x+4)(x-2) \neq 0$
 $x \neq -4 \quad x \neq 2$

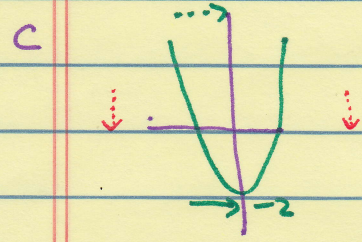
14 $y = |x|$



D: all real #s
R: $y \geq 0$



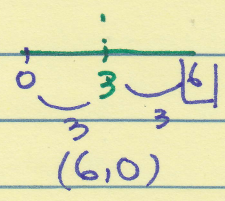
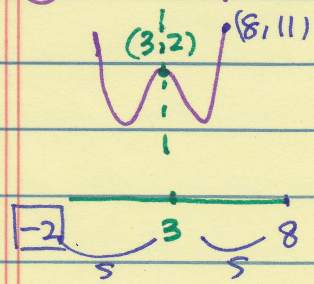
D: all real #s
R: $-1 \leq y \leq 1$



D: all real #s
R: $y \geq -2$

15 b & d because they both pass the horizontal & vertical line test and hence are one-to-one

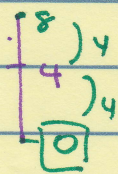
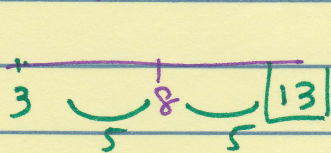
16. (a) line symmetry



$(-2, 1)$

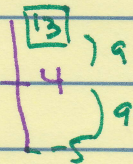
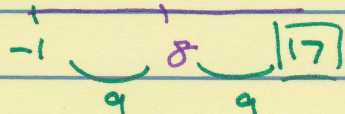
16b Point symmetry: $(8, 4)$

$(3, 8)$



$(3, 8) \rightarrow (13, 0)$

$(-1, -5)$



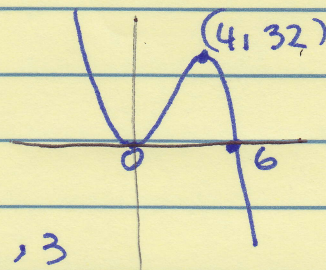
$(-1, -5) \rightarrow (17, 13)$

p. 144

13. $g(x) = f(2x) \rightarrow$ half your x

local max $(2, 32)$

zeros: $\frac{0}{2}, \frac{6}{2}$ or $0, 3$



b. $y = 2f(x)$ dbl y values

local max $(4, 32)(2) = (4, 64)$

zeros: $0, 6$ (y values remain zero)

c. $y = f(x-2) \rightarrow$ add 2 to x .

local max: $(4+2, 32) = (6, 32)$

zeros: $0+2; 6+2$ or $2; 8$

d. $y = f(x+2) \rightarrow$ subtract 2 from x

local max: $(4-2, 32)$ or $(2, 32)$

zeros: $0-2; 6-2$ or $-2; 4$