

Two events are *independent* if one event has no effect on the other. Two events are *dependent* if one event affects the other.

If A and B are independent events, then $P(A \text{ and } B) = P(A) \cdot P(B)$.

If A and B are dependent events, then $P(A \text{ and } B) = P(A) \cdot P(B|A)$.

$P(B)$ depending A

Example 1 There are 3 red pens, 4 blue pens, and 5 black pens in a box.

- (a) Suppose you choose 2 pens at random (one at a time) with replacement. Find the probability of choosing blue, then black.

$$\frac{4}{12} \times \frac{5}{12} = \frac{5}{36}$$

independent

- (b) Suppose you choose 3 pens at random (one at a time) without replacement. Find the probability of choosing red, then blue, then blue.

$$\frac{3}{110} = \frac{P(\text{red})}{\frac{3}{12}} \times \frac{P(\text{Blue})}{\frac{4}{11}} \times \frac{P(\text{Blue})}{\frac{3}{10}}$$

dependent

Example 2 The probability it will rain on a certain day is 10% in Placentia and 20% in Laguna Beach. Find the probability it will rain in at least one of these cities.

$$P_{\text{yes}} \& L_{\text{no}} \text{ OR } L_{\text{yes}} \& P_{\text{no}} \text{ OR } P_{\text{yes}} \& L_{\text{yes}}$$

$$(.1)(.8) + (.2)(.9) + (.1)(.2) = .28 = 28\%$$

Example 3 In a survey of adults 35-60 years old, 45% were men. Twenty percent of the men surveyed admitted they watched infomercials, and 48% of the women admitted to watching infomercials. Use a tree diagram to find the probability that a randomly selected adult watches infomercials.

