

5.2 Factoring Trinomials/Solving by Factoring

Keys to successful factoring:



Arrange trinomial in descending/ascending degree



Factor out the greatest common factor to reduce the size of the exponents or coefficients, or to eliminate fractions



Check your factoring with multiplication

$$\frac{2}{3}x^2 - 20$$

Factor completely:

ex. 1 $-3x^2 + 36x + 84$
 $-3(x^2 - 12x - 28)$
 $-3(x+2)(x-14)$

ex. 2 $x^{2n} - 12x^n + 27$
 $x^{2n} = (x^n)^2$
 $(x^n - 9)(x^n - 3)$

ex. 3 $(x-4)^2 - 5(x-4) - 150$

$$((x-4) - 15)((x-4) + 10)$$

$$(x-19)(x+6)$$

ex. 4 $2x^2 + 11x + 15$

$$(2x+5)(x+3)$$

ex. 5 $3x^3 - 10x^2 - 8x$

$$= x(3x^2 - 10x - 8)$$

$$= x(3x+2)(x-4)$$

ex. 6 $4x^2 - 27x + 18$

prod $72x^2$
sum $-27x$

$(x-6)(4x-3)$

$-3x, -24x$

$-24x$

$-3x$

ex. 7 $6x^2 - 17x - 10$

$(3x-10)(2x+1)$

$-60x^2$
prod
sum
 $-17x$
 $-20x, 3x$

Zero Product Property: If $ab = 0$, then $a = 0$ or $b = 0$.

ex. 8 Solve for x.

$30x^3 = 57x^2 - 21x$

$30x^3 - 57x^2 + 21x = 0$

$3x(10x^2 - 19x + 7) = 0$

$3x(5x-7)(2x-1) = 0$

$3x=0$ OR $5x-7=0$ OR $2x-1=0$

$\rightarrow x = 0, \frac{7}{5}, \frac{1}{2}$