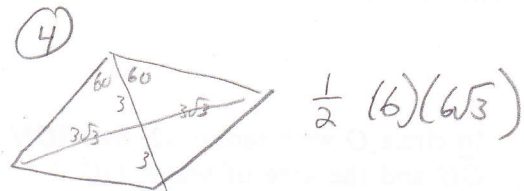


Areas of Plane Figures

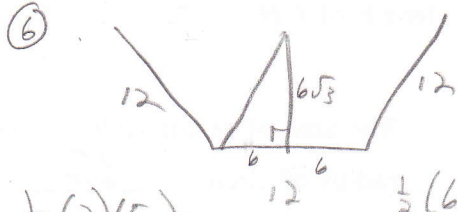
For use after Chapter 11

Find the area of each figure described.

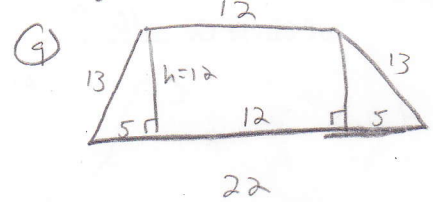
- A rectangle with length 15 and width 12 180 un²
- A parallelogram with base 18 and height 9 162 un²
- A triangle with base 13 and height 8 52 un²
- A rhombus with shorter diagonal 6 cm and a 120° angle 18√3 un²
- A square whose perimeter is 60 225 un²
- A regular hexagon with side 12 216√3 un²
- A regular pentagon with side s and apothem 3 7.5s un²
- A rhombus with diagonals 6 and 14 42 un²
- An isosceles trapezoid with legs 13 and bases 12 and 22 204 un²



$$\frac{1}{2} (6)(6\sqrt{3})$$



$$\frac{1}{2} (3)(15s)$$



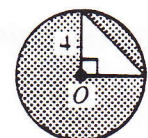
$$\frac{1}{2} (12)(12+22)$$

$$\boxed{204}$$

- Find the circumference and area of a circle with radius 10. Use $\pi \approx 3.14$.
 $C \approx \underline{62.8}$, $A \approx \underline{314}$

ii) $r=10$, $C=24\pi$
 $d=24$

- The area of a circle is 144π . Find the circumference. 24π



Ex. 12

12) $A_{\text{circle}} - A_{\Delta}$
 $16\pi - \frac{1}{2}(4 \cdot 4)$
 $16\pi - 8$

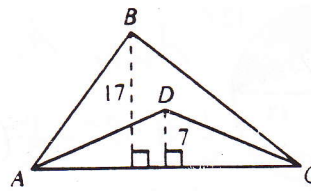
- Find the area of the shaded region of $\odot O$. 16π - 8
- In circle P with diameter 10, $m\angle APB = 60$. Find the length of \widehat{AB} and the area of sector APB.

length of $\widehat{AB} = \frac{5\pi}{3}$, $A = \frac{25\pi}{6}$

- The ratio of the areas of two rectangles is 36 : 64. Find the scale factor and the ratio of the perimeters.
 scale factor = 3:4, ratio of the perimeters = 3:4

- Two similar polygons have scale factor 3 : 4. The area of the smaller polygon is 108. Find the area of the larger polygon.
192 $\frac{9}{16} = \frac{108}{x}$ $9x = 1728$
 $x = 192$

- The ratio of the areas of $\triangle ABC$ and $\triangle ADC$ is 17:7.



$$\frac{1}{6} \cdot 2 \cdot \pi \cdot 5^2$$

$$\frac{1}{6} \cdot \pi \cdot 5^2$$

- The areas of two circles are 144π and 64π . The ratio of their circumferences is 3:2.

Ratio of $A = \frac{144\pi}{64\pi} = \frac{144}{64} = \frac{36}{16} = \frac{9}{4}$

- The ratio of the perimeters of two similar triangles is 3 : 5. The scale factor is 3:5 and the ratio of their areas is 9:25.

#1

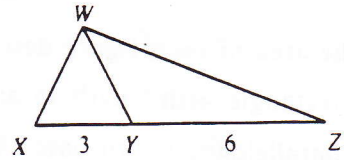
$\tan 36^\circ = \frac{x}{3}$
 $1 \text{ side} = 2x = 4.36$
 $P = (1.5) = 21.8$
 $A = \frac{1}{2} (3)(21.8) \approx 32.7$ $x \approx 2.18$

19. Two similar polygons have scale factor 3 : 5. The area of the larger polygon is 125.

The area of the smaller polygon is 45.

$$\frac{9}{25} = \frac{x}{125} \quad 25x = 1125$$

20. The ratio of the areas of $\triangle WXY$ and $\triangle WYZ$ is 1:2.



21. In circle O with radius 12, $m\angle GOH = 30$. Find the length of \widehat{GH} and the area of sector GOH .

length of $\widehat{GH} = \underline{2\pi}$, $A = \underline{12\pi}$

$$\frac{30}{360} = \frac{1}{12} \cdot 2 \cdot \pi \cdot 12$$

$$\frac{1}{12} \cdot \pi \cdot 12^2$$

22. The area of sector AOB is 20π and $m\angle AOB = 100$. Find the radius of circle O . $6\sqrt{2}$ (8.49)

$$20\pi = \frac{100}{360} \cdot \pi \cdot r^2$$

23. The length of \widehat{CD} is 4.2π and $m\angle COD = 70$. Find the radius of circle O . 10.8

$$20\pi = \frac{5}{18} \cdot \pi \cdot r^2$$

$$20 = \frac{5}{18} \cdot r^2$$

$$72 = r^2$$

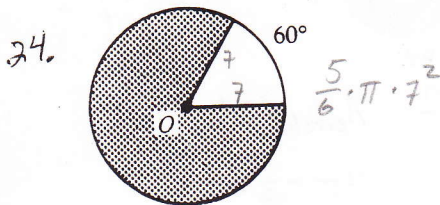
$$r = \sqrt{72}$$

$$r = 6\sqrt{2}$$

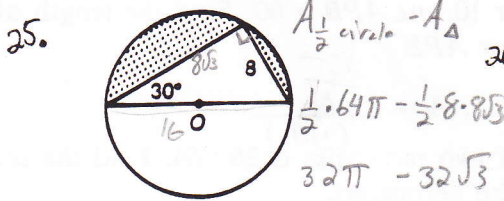
$$4.2 = \frac{7}{18} \cdot r \quad 4.2\pi = \frac{70}{360} \cdot 2\pi r$$

$$10.8 = r \quad 4.2\pi = \frac{7}{36} \cdot 2\pi r$$

Find the area of each shaded region. Point O marks the center of a circle.



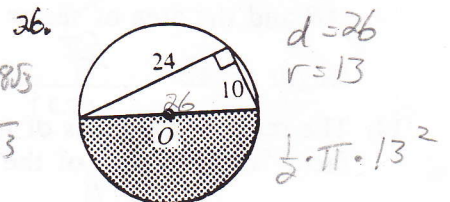
$$\frac{5}{6} \cdot \pi \cdot 7^2$$



$$A_{\frac{1}{2} \text{ circle}} - A_{\Delta}$$

$$\frac{1}{2} \cdot 64\pi - \frac{1}{2} \cdot 8 \cdot 8\sqrt{3}$$

$$32\pi - 32\sqrt{3}$$



$$d = 26$$

$$r = 13$$

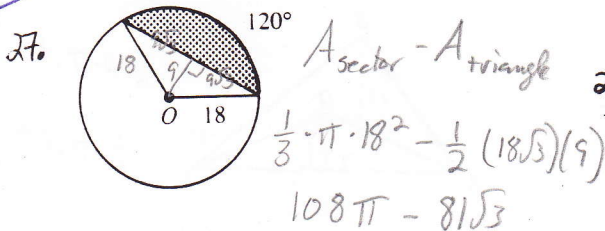
$$\frac{1}{2} \cdot \pi \cdot 13^2$$

24. $A = \frac{245\pi}{6}$ OR $46\frac{5}{6}\pi$ OR $49\pi - \frac{49\pi}{6}$

25. area = $32\pi - 32\sqrt{3}$

45.11

26. $A = \frac{169\pi}{2}$ 84.5π

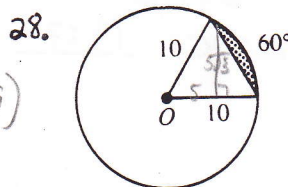


$$A_{\text{sector}} - A_{\text{triangle}}$$

$$\frac{1}{3} \cdot \pi \cdot 18^2 - \frac{1}{2} (18\sqrt{3})(9)$$

$$108\pi - 81\sqrt{3}$$

27. $A = \underline{108\pi - 81\sqrt{3}}$



$$A = \frac{50\pi}{3} - 25\sqrt{3}$$

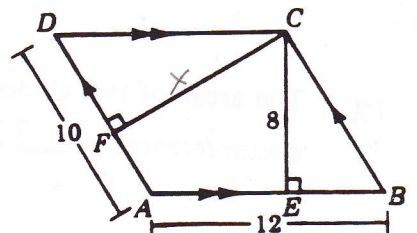
$$A_{\text{sector}} - A_{\Delta}$$

$$\frac{1}{6} \cdot \pi \cdot 10^2 - \frac{1}{2} \cdot (10)(5\sqrt{3})$$

$$\frac{100\pi}{6} - \frac{1}{2} (50\sqrt{3})$$

7.06

29) find CF. 265.46



$$A_{\square} = 8 \cdot 12 = 96$$

$$CF = \underline{9.6} \quad 96 = 10 \cdot x$$

19 8.996