

Equations of Lines

May 17

★ slope-intercept form: $y = mx + b$

ex. 1: y-intercept = -2 and perpendicular to $y = -8x + 9$

$$y = \frac{1}{8}x - 2$$

⊥ slope = $\left(\frac{1}{8}\right)$ (neg. reciprocal)
slope

ex. 2: slope = $\frac{2}{3}$, point on line = $(-6, 4)$

$$y = \frac{2}{3}x + 8$$

$$\begin{aligned} y &= mx + b \\ 4 &= \frac{2}{3}(-6) + b \\ 4 &= -4 + b \\ 8 &= b \end{aligned}$$

★ point-slope form: $y - y_1 = m(x - x_1)$

~~$m = \frac{y - y_1}{x - x_1}$~~
slope

$m = \text{slope}$

(x_1, y_1) Known pt
 (x, y) all other pts

ex. 3: parallel to the line $y = -3x - 2$, point on line $(4, -5)$

$m = -3$ (= slopes) $(x_1, y_1) = (4, -5)$

$y - y_1 = m(x - x_1)$
 $y - (-5) = -3(x - 4)$
 $y + 5 = -3(x - 4)$
 $\rightarrow y = -3x + 12 - 5$
 $y = -3x + 7$

ex. 4: points $(1, -2)$ and $(-3, 5)$ on line

$m = \frac{-2 - 5}{1 - (-3)} = \frac{\text{rise}}{\text{run}} = -\frac{7}{4}$

$(x_1, y_1) = (1, -2)$
 $y = -\frac{7}{4}x - \frac{1}{4}$

$y - y_1 = m(x - x_1)$
 $y - (-2) = -\frac{7}{4}(x - 1)$
 $y + 2 = -\frac{7}{4}x + \frac{7}{4} - \frac{8}{4}$