

**math induction #2**    Prove by induction:  $\sum_{i=1}^n (2i-1) = n^2$

1. For  $n = 1$ ,  $2(1) - 1 = 1^2$   
 $1 = 1$

2. Assume that  $1 + 3 + 5 + \dots + (2(k-1) - 1) = (k-1)^2$ .

3. Show that  $1 + 3 + 5 + \dots + (2k - 1) = k^2$ .

**Proof:**  $1 + 3 + 5 + \dots + (2k - 3) = k^2 - 2k + 1$   
 $1 + 3 + 5 + \dots + (2k - 3) + (2k - 1) = k^2 - 2k + 1 + (2k - 1)$   
 $= k^2$

Prove by induction:  $\sum_{i=1}^n \frac{1}{i(i+1)} = \frac{n}{n+1}$

math induction #3

1. For  $n = 1$ :  $\frac{1}{1(1+1)} = \frac{1}{1+1}$   
 $\frac{1}{1(2)} = \frac{1}{2}$   
 $\frac{1}{2} = \frac{1}{2}$

2. Assume that

$$\frac{1}{1(2)} + \frac{1}{2(3)} + \frac{1}{3(4)} + \dots + \frac{1}{\underline{(k-1)}(\underline{k-1+1})} = \frac{\underline{k-1}}{\underline{(k-1)+1}}$$

3. Show that

$$\frac{1}{1(2)} + \frac{1}{2(3)} + \frac{1}{3(4)} + \dots + \frac{1}{k(k+1)} = \frac{k}{k+1}$$

**Proof:**

$$\frac{1}{1(2)} + \frac{1}{2(3)} + \frac{1}{3(4)} + \dots + \frac{1}{(k-1)(k)} = \frac{k-1}{k}$$

$$\begin{aligned} \frac{1}{1(2)} + \frac{1}{2(3)} + \frac{1}{3(4)} + \dots + \frac{1}{(k-1)(k)} + \frac{1}{k(k+1)} &= \frac{k-1}{k} + \frac{1}{k(k+1)} \\ &= \frac{(k-1)(k+1) + 1}{k(k+1)} \\ &= \frac{k^2 - 1 + 1}{k(k+1)} \\ &= \frac{k^2}{k(k+1)} \\ &= \frac{k}{k+1} \end{aligned}$$