

USING DIMENSIONAL ANALYSIS

Solve the following problems using dimensional analysis. Express your answers in scientific notation with a maximum of three significant figures in boxes.

Convert these quantities into MKS units. We'll start with easy ones.

1. 0.87 minutes
2. 37 grams
3. 17.5 minutes
4. 7,070 lightyears

These next few conversions require more fractions.

5. 9.6 micrograms
6. 765 hours
7. 3.09 days
8.  $7.56 \times 10^{-6}$  years

Use the handout on approximate values to solve these problems.

9. How many times longer is a human life than the life of an unstable nucleus?

10. How many heartbeats are there in a typical human life span?
11. How many lightyears is it to the Andromeda Galaxy from Earth?
12. If the Sun's mass is about average for stars (which it isn't), how many stars are in the Milky Way Galaxy?
13. If we assume that the Sun is pure hydrogen (which it isn't), how many hydrogen atoms are in the Sun?
14. If a beam of light was produced at the edge of the known universe, how many years would it take to reach Earth?
15. If a hydrogen atom contains only one proton and one electron, what is the mass of a proton? How much more massive than an electron is a proton?
16. How many FM radio waves could pass through your brain during a single nerve impulse? Does this indicate why the human brain incapable of detecting radio waves?

TABLE 1.3

## APPROXIMATE VALUES OF LENGTH, MASS, AND TIME

*Lengths in meters*

$10^{-17}$	Present experimental limit to smallest observable detail
$10^{-15}$	Diameter of proton
$10^{-14}$	Diameter of uranium nucleus
$10^{-10}$	Diameter of hydrogen atom
$10^{-8}$	Thickness of membranes in cells of living organisms
$10^{-6}$	Wavelength of visible light
$10^{-3}$	Size of grain of sand
1	Height of a 4-year-old child
$10^2$	Length of a football field
$10^4$	Greatest ocean depth
$10^7$	Diameter of the earth
$10^{11}$	Distance from the earth to the sun
$10^{16}$	Distance traveled by light in 1 year (a light year)
$10^{21}$	Diameter of the Milky Way galaxy
$10^{22}$	Distance from earth to nearest large galaxy (Andromeda)
$10^{26}$	Distance from earth to edge of the known universe

$$\text{Range of lengths} = 10^{26}/10^{-17} = 10^{43}$$

*Masses in kilograms**(more precise values in parentheses)*

$10^{-30}$	Mass of an electron ( $9.11 \times 10^{-31}$ kg)
$10^{-27}$	Mass of a hydrogen atom ( $1.67 \times 10^{-27}$ kg)
$10^{-15}$	Mass of a bacterium
$10^{-5}$	Mass of a mosquito
$10^{-2}$	Mass of a hummingbird
1	Mass of a liter of water (about a quart)
$10^2$	Mass of a person
$10^3$	Mass of a car
$10^8$	Mass of a large ship
$10^{12}$	Mass of a large iceberg
$10^{15}$	Mass of the nucleus of a comet
$10^{23}$	Mass of the moon ( $7.36 \times 10^{22}$ kg)
$10^{25}$	Mass of the earth ( $5.98 \times 10^{24}$ kg)
$10^{30}$	Mass of the sun ( $1.99 \times 10^{30}$ kg)
$10^{42}$	Mass of the Milky Way galaxy (current upper limit)
$10^{53}$	Mass of the known universe (current upper limit)

$$\text{Range of masses} = 10^{53}/10^{-30} = 10^{83}$$

*Times in seconds**(more precise values in parentheses)*

$10^{-23}$	Time for light to cross a proton
$10^{-22}$	Mean life of an extremely unstable nucleus
$10^{-15}$	Time for one oscillation of visible light
$10^{-13}$	Time for one vibration of an atom in a solid
$10^{-8}$	Time for one oscillation of an FM radio wave
$10^{-3}$	Duration of a nerve impulse
1	Time for one heartbeat
$10^5$	One day ( $8.64 \times 10^4$ s)
$10^7$	One year ( $3.16 \times 10^7$ s)
$10^9$	About half the life expectancy of a human
$10^{11}$	Recorded history
$10^{17}$	Age of the earth
$10^{18}$	Age of the universe

$$\text{Range of times} = 10^{18}/10^{-23} = 10^{41}$$

