

Extra Examples Sec. 3-3

① use long division

$$(16x^4 + 40x^3 - 8x^2 - 14x + 15) \div (2x + 5)$$

$$\begin{array}{r}
 8x^3 \quad -4x + 3 \\
 \hline
 \cancel{2x+5} \overline{) 16x^4 + 40x^3 - 8x^2 - 14x + 15} \\
 \underline{-(16x^4 + 40x^3)} \\
 -8x^2 - 14x = 8x^3 - 4x + 3 \\
 \underline{-(-8x^2 - 20x)} \\
 6x + 15 \\
 \underline{-(6x + 15)} \\
 0
 \end{array}$$

② divide using synthetic division

$$(x^4 - 6x^3 + 0x^2 - 40x + 33) \div (x + 7)$$

$$\begin{array}{r|rrrrr}
 -7 & 1 & -6 & 0 & -40 & 33 \\
 & & -7 & 91 & -637 & 4739 \\
 \hline
 & & -13 & 91 & -677 & 4772
 \end{array}$$

$$x^3 - 13x^2 + 91x - 677 + \frac{4772}{x+7}$$

③ use synthetic substitution

to evaluate $f(x)$ when $x = -3$

$$f(x) = x^3 + 2x^2 - 6x - 15 \quad x = -3$$

$$\begin{array}{r|rrrr}
 -3 & 1 & 2 & -6 & -15 \\
 & & -3 & 3 & 9 \\
 \hline
 & 1 & -1 & -3 & -6 \\
 & x^2 & -x & -3 & -\frac{6}{x+3}
 \end{array}$$