

Warm-Up

Number	Occurrences
1	26
2	10
3	12
4	9
5	14
6	29

100 total rolls

$$\frac{55}{100}$$

1. The table shows the results of rolling a die with unequal faces. Find the experimental probability of rolling 1 or 6.
2. Find the experimental probability of rolling a number greater than 3.  $\frac{52}{100}$
3. Find the theoretical probability of rolling a 5  $\frac{1}{6}$

# 7.3

## Independent and Dependent Events

Two events are **independent** if the occurrence of one has no effect on the occurrence of the other.

If A and B are independent events, then the probability that both A and B occur is:

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

This also works with 3 or more events:

$$P(A \text{ and } B \text{ and } C) = P(A) \cdot P(B) \cdot P(C)$$

1) If you flip a coin 8 times, and the first seven all were "heads", what is the probability that the 8<sup>th</sup> flip will be heads?

$$\frac{1}{2}$$

2) What is the probability that you flip a coin and it lands on "heads" 8 times in a row?

$$\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \left(\frac{1}{2}\right)^8$$

You are playing a game with 2 numbered cubes. Find the probability of rolling a sum of 8 on the first roll and doubles on the second roll.

$$\frac{5}{36} \cdot \frac{6}{36}$$

Find the probability of rolling an even sum on the first roll and a sum greater than 8 on the second roll.

$$\frac{18}{36} \cdot \frac{18}{36} = \frac{5}{36}$$

A game machine claims that 1 in every 15 people win. What is the probability that you win <sup>three</sup> times in a row?

$$\frac{1}{15} \cdot \frac{1}{15} \cdot \frac{1}{15}$$

Two events A and B are **dependent events** if the occurrence of one affects the occurrence of the other.

The probability that B will occur given that A has occurred is called the **conditional probability** of B given A and is written P(B/A).

If A and B are dependent events, then the probability that both A and B occur is:

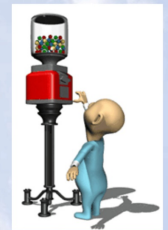
$$P(A \text{ and } B) = P(A) \cdot P(B/A)$$

↑  
given

A gumball machine contains 100 gumballs, twenty of each of the colors red, blue, green, white, and yellow.

What is the probability of getting a blue gumball then a white gumball.

$$\frac{20}{100} \cdot \frac{20}{99} = \frac{4}{99}$$



A gumball machine contains 100 gumballs, twenty of each of the colors red, blue, green, white, and yellow.

What is the probability of getting a green, then red, then blue gumball.

$$\frac{20}{100} \cdot \frac{20}{99} \cdot \frac{20}{98}$$



A gumball machine contains 100 gumballs, twenty of each of the colors red, blue, green, white, and yellow.

What is the probability of getting a blue, then blue, then blue gumball.

$$\frac{20}{100} \cdot \frac{19}{99} \cdot \frac{18}{98}$$



A gumball machine contains 100 gumballs, twenty of each of the colors red, blue, green, white, and yellow.

What is the probability of getting a yellow, then another yellow gumball.

$$\frac{20}{100} \cdot \frac{19}{99}$$



You randomly select 2 cards from a standard 52-card deck. What is the probability that both cards are face cards (king, queen, or jack)?

a) you replace the first card before selecting the 2<sup>nd</sup> (with replacement)

$$\frac{12}{52} \cdot \frac{12}{52}$$

b) you do not replace the first card (without replacement)

$$\frac{12}{52} \cdot \frac{11}{51}$$