

5-4 Complex Numbers

Alg 2 standards
5.0 and 6.0

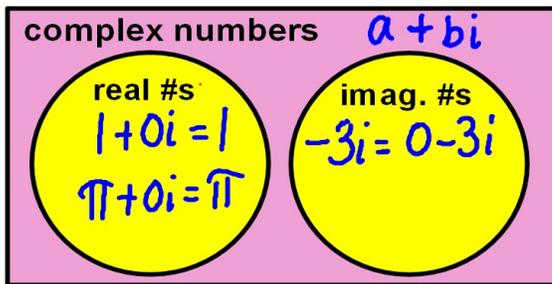
i is the **imaginary unit**

$$i = \sqrt{-1}$$

$$i^2 = -1$$

$a + bi$ is a **complex number** in standard form

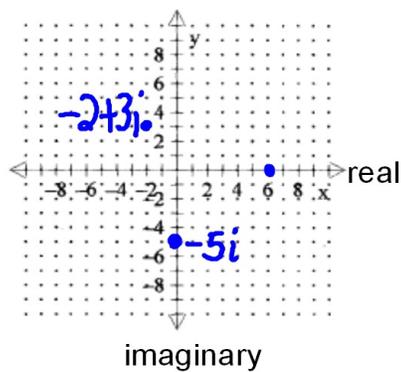
a is the real part and bi is the imaginary part



ex. 1

graph $-2 + 3i$ and $-5i$ in the complex plane

$$6 = 6 + 0i$$



Simplify:

ex. 2

$$2i - (3 + 4i) + (8 - 9i) \\ 2i - 3 - 4i + 8 - 9i = 5 - 11i$$

ex. 3

$$\sqrt{-32} = \sqrt{-1} \cdot \sqrt{32} = i \cdot 4\sqrt{2} = 4\sqrt{2}i \\ 4i\sqrt{2}$$

ex. 4

$$\sqrt{-20} \cdot \sqrt{-3} = i^2 \cdot 2\sqrt{15} = -2\sqrt{15} \\ \frac{i\sqrt{20}}{2\sqrt{5}} \cdot i\sqrt{3} = \frac{i^2}{(-1)} \cdot 2\sqrt{15} = -2\sqrt{15}$$

ex. 5

$$\sqrt{\frac{-3}{8}} = \frac{i\sqrt{3}}{2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{i\sqrt{6}}{4} \text{ or } \frac{\sqrt{6}}{4}i$$

ex. 6

$$i^{14} = (i^2)^7 = (-1)^7 = -1$$

ex. 7

$$i^{77} = (i^2)^{38} \cdot i = (-1)^{38} i = i$$

Solve for x over the complex numbers:

ex. 8

$$5(x-3)^2 = -20 \\ \sqrt{(x-3)^2} = \sqrt{-4} \quad i\sqrt{4} \\ x-3 = \pm 2i \\ x = 3 \pm 2i$$