

Chapter 11 Review

Although the following formulas will be provided on the exam, you still need to know when to use a specific formula.

$$a_n = a_1 r^{n-1}$$

$$a_n = a_1 + (n-1)d$$

$$S_n = n \left(\frac{a_1 + a_n}{2} \right)$$

$$S = \frac{a_1}{1-r}$$

$$S_n = a_1 \left(\frac{1-r^n}{1-r} \right)$$

1) Fill in the following table with the above formulas:

	ARITHMETIC	GEOMETRIC
Rule OR General Term of a Sequence	$a_n = a_1 + (n-1)d$	$a_n = a_1 r^{n-1}$
Sum of First n Terms in a Series	$S_n = n \left(\frac{a_1 + a_n}{2} \right)$	$S_n = a_1 \left(\frac{1-r^n}{1-r} \right)$

Identify whether the sequence is *arithmetic*, *geometric*, or *neither*. Then write its general term (or rule).

2) 1, 0, -2, -5, ... **N**

3) 2, -2, 2, -2, ... **G**
 $a_n = 2(-1)^{n-1}$

4) 1, -2, -5, -8 **A**
 $a_n = 4 - 3n$

5) 1, -2, 3, -4, ... **N**

Find the term given the rule of the sequence.

6) The tenth term in $a_n = 17 - 5n$ **-33**

8) The first term in $a_n = 3n + 1$ **4**

7) The 23rd term in $a_n = 3 - 2n$ **-43**

First identify whether the series is finite or infinite. Then write the series using summation notation:

F 9) $1 + 5 + 9 + 13 + 17$ **$\sum_{n=1}^5 -3 + 4n$**

10) $-3 + 3 + 9 + 15 + 21 + \dots$ **Inf.**
 $\sum_{n=1}^{\infty} -9 + 6n$

11) $7 + 8 + 9 + 10 + 11 + 12$ **F**
 $\sum_{n=7}^{12} n$

Expand using summation notation and find the sum:

12) $\sum_{n=1}^6 3n$ **63**

13) $\sum_{n=0}^4 n^2$ **30**

14) $\sum_{k=1}^5 (k^2 - 1)$ **50**

15) $\sum_{n=1}^5 \frac{n}{n+1}$ **3.55**

Write the general term (rule) of each sequence:

16) 5, 10, 20, 40, ...

$$a_n = 5(2)^{n-1}$$

17) -1, 0, 1, 2, ...

$$a_n = n - 2$$

18) $2, \frac{4}{3}, \frac{8}{9}, \dots$

$$a_n = 2\left(\frac{2}{3}\right)^{n-1}$$

Find the A) sum of the first n terms of each arithmetic series and B) find the n for the given s_n

19) $2+3+4+5+6+\dots$

$n = 20$

$s_n = 5,150$

230; 100

21) $2 + \frac{5}{2} + 3 + \frac{7}{2} + 4 + \dots$

$n = 50$

$s_n = 1,005$

712.5
60

20) $25+35+45+55+\dots$

$n = 15$

$s_n = 3,105$

1425; 23

22) $9+13+17+21+25+\dots$

$n = 14$

$s_n = 2,272$

490; 32

Find the A) sum of the first n terms of each geometric series and B) find the n for the given s_n

23) $1+(-4)+16+(-64)+\dots$

$n = 20$

$s_n = 5,150$

13,107
6

25) $1+4+16+64+\dots$

$n = 10$

$s_n = 21,845$

349,525
8

24) $-2+3+(-\frac{9}{2})+\frac{27}{4}+\dots$

$n = 14$

$s_n = -31.55$

-232.74; 9

Write the general term (rule) of each sequence:

26) $a_1 = \frac{37}{3}; d = \frac{5}{3}$

$a_n = \frac{32}{3} + \frac{5}{3}n$

29) $a_1 = 4; r = \frac{1}{8}$

$a_n = 4\left(\frac{1}{8}\right)^{n-1}$

27) $a_1 = 45; r = \frac{1}{3}$

$a_n = 45\left(\frac{1}{3}\right)^{n-1}$

30) $d = 8; a_1 = -14$

$a_n = -22 + 8n$

28) $d = -6; a_1 = 62$

$a_n = 68 - 6n$

31) $r = \frac{1}{2}; a_1 = -40$

$a_n = -40\left(\frac{1}{2}\right)^{n-1}$

Find the sum of the infinite geometric series if it has one.

32) $\sum_{n=1}^{\infty} 4\left(-\frac{1}{3}\right)^{n-1}$

3

33) $\sum_{n=0}^{\infty} 2\left(\frac{5}{4}\right)^n$

no sum

34) $\sum_{n=0}^{\infty} -7\left(\frac{1}{3}\right)^n$

-21/2

35) $\sum_{n=1}^{\infty} -4\left(\frac{1}{6}\right)^{n-1}$

-24/5

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Find the common ratio of the infinite geometric series with the given sum and first term.

36) $S = 4$
 $a_1 = 7$ $-3/4$

37) $S = \frac{8}{9}$
 $a_1 = \frac{2}{3}$ $1/4$

38) $S = \frac{16}{3}$
 $a_1 = 8$ $-1/2$