

Simplify

1.  $\csc^2 \theta - \cot^2 \theta$

2.  $\frac{\tan(-\theta)}{\sec \theta}$

3.  $\tan(-\alpha)\cos(-\alpha)$

4.  $\cot^2 x(1 + \tan^2 x)$

5.  $\tan^2 \theta - \frac{\sec^2 \theta}{\csc^2 \theta}$

6.  $\frac{\tan x \csc x}{\sec x}$

7.  $\sec \theta + \tan \theta$

8.  $\frac{\sec \alpha}{\tan \alpha + \cot \alpha}$

9.  $\sec^2 x - \tan^2 x$

10.  $\csc^2 y + \sec^2 y$

11.  $\cot^2 x - \csc^2 x$

12.  $1 + \cot^2 \alpha$

13.  $\frac{1 + \tan^2 \theta}{\tan^2 \theta}$

14.  $\frac{1 - \sin^2 t}{\csc^2 t}$

15.  $\cot^2 \theta \sin^2 \theta + \tan^2 \theta \cos^2 \theta$

16.  $\frac{1 + \tan^2 \theta}{1 + \cot^2 \theta}$

17.  $\frac{\cot^2 \theta - \csc^2 \theta}{\cos^2 \theta}$

Prove the identity.

$$18. \cot x + \tan x = \csc x \cdot \sec x$$

$$19. \frac{\sin \alpha}{\csc \alpha + \cot \alpha} = 1 - \cos \alpha$$

$$20. \frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = 2 \csc \theta$$

$$21. \tan x - \cot x = \frac{\sin^2 x - \cos^2 x}{\sin x \cos x}$$

Answers:

1. 1

2.  $-\sin \theta$

3.  $-\sin \alpha$

4.  $\csc^2 x$

5. 0

6. 1

7.  $\frac{1 + \sin \theta}{\cos \theta}$

8.  $\sin \alpha$

9. 1

10.  $\csc^2 y \sec^2 y$

11. -1

12.  $\csc^2 \alpha$

13.  $\csc^2 \theta$

14.  $\sin^2 t \cos^2 t$

15. 1

16.  $\tan^2 \theta$

17.  $-\sec^2 \theta$