

Oct. 10, 2013

Extra Examples Section 3-4 and 3-5

① Find all real solutions.

$$8x^4 - 30x^2 + 7 = 0 \quad x^2 =$$

prod = $56x^4$
sum = $-30x^2$
 $-28x^2, -2x^2$

$$(4x^2 - 1)(2x^2 - 7) = 0$$

$$\begin{aligned} 4x^2 - 1 &= 0 & 2x^2 - 7 &= 0 \\ 4x^2 &= 1 & 2x^2 &= 7 \\ x^2 &= \frac{1}{4} & \sqrt{x^2} &= \frac{\sqrt{7}}{\sqrt{2}} \\ x &= \pm \frac{1}{2} & x &= \pm \frac{\sqrt{14}}{2} \end{aligned}$$

② Find all real solutions.

$$64x^3 = 27$$

$$\begin{aligned} 64x^3 - 27 &= 0 \\ (4x - 3)(16x^2 + 12x + 9) &= 0 \\ x &= \frac{3}{4} \end{aligned}$$

$$\sqrt[3]{x^3} = \sqrt[3]{\frac{27}{64}} \quad x = \frac{3}{4}$$

③

Factor $p(x)$ given that $p(a) = 0$.

$$p(x) = 2x^3 + 7x^2 - 33x - 18; \quad a = -6$$

$$\begin{array}{r|rrrr} -6 & 2 & 7 & -33 & -18 \\ & & -12 & 30 & 18 \\ \hline & 2 & -5 & -3 & 0 \end{array}$$

$$(x+6)(2x^2 - 5x - 3) = (x+6)(2x+1)(x-3)$$