

5-5 COMPLETING THE SQUARE

Trinomial Squares $A^2 + 2AB + B^2 = (A + B)^2$
 $A^2 - 2AB + B^2 = (A - B)^2$

ex. 1 Complete the trinomial squares and factor.

a) $x^2 - 16x + 64 = (x - 8)^2$
 $(x)^2 - 2(8)(x) + (8)^2$

b) $x^2 + 50x + 625 = (x + 25)^2$
 $(x)^2 + 2(25)(x) + (25)^2$

c) $x^2 + 7x + \frac{49}{4} = \left(x + \frac{7}{2}\right)^2$
 $(x)^2 + 2\left(\frac{7}{2}\right)(x) + \left(\frac{7}{2}\right)^2$

Solve by completing the square (CTS)

ex. 2 $x^2 + 6x - 8 = 0$

$$x^2 + 6x + 9 = 8 + 9$$

$$\sqrt{(x+3)^2} = \sqrt{17}$$

$$x + 3 = \pm\sqrt{17}$$

$$x = -3 \pm \sqrt{17}$$

ex. 3 $x^2 - 12x + 44 = 0$

$$x^2 - 12x + 36 = -44 + 36$$

$$\sqrt{(x-6)^2} = \sqrt{-8}$$

$$x - 6 = \pm 2i\sqrt{2}$$

$$x = 6 \pm 2i\sqrt{2}$$

ex. 4

$$4x^2 - 12x + 4 = 0$$

$$x^2 - 3x + \frac{9}{4} = -1 + \frac{9}{4}$$

$$\sqrt{\left(x - \frac{3}{2}\right)^2} = \sqrt{\frac{5}{4}}$$

$$x - \frac{3}{2} = \frac{\pm\sqrt{5}}{2}$$

$$x = \frac{3 \pm \sqrt{5}}{2} \quad \text{or} \quad \frac{3}{2} \pm \frac{\sqrt{5}}{2}$$