

Distance Formula:

distance traveled = rate of speed x time traveled

$$d = r t$$

$$\text{so } t = \frac{d}{r}$$

Example 1: Backwoods Sam can paddle his canoe 50 miles upstream against the current in the same time he can paddle 75 miles downstream with the current. The current is flowing at 3 miles per hour. Find Sam's paddling rate in still water.

	r	\cdot	t	$=$	d
Upstream	$p - 3$	\cdot	$\frac{50}{p - 3}$	$=$	50
Downstream	$p + 3$	\cdot	$\frac{75}{p + 3}$	$=$	75

$p =$ paddling rate

$$\frac{50}{p - 3} = \frac{75}{p + 3}$$

$$50p + 150 = 75p - 225$$

$$375 = 25p$$

$$\boxed{15^{\text{mph}} = p}$$

Work formula:

work done = rate of work (per unit of time) x time on job

$$w = r t$$

Example 2. Jeff can build a brick wall in 5 days. Sergio can build the same wall in 4 days. Working together, how long will it take them to build the wall?

	(per day)	\cdot	(on job)	$=$	w
Jeff	$\frac{1}{5}$	\cdot	x	$=$	$\frac{x}{5}$
Sergio	$\frac{1}{4}$	\cdot	x	$=$	$\frac{x}{4}$

$x =$ time both on job

$$20 \left(\frac{x}{5} + \frac{x}{4} = 1 \right) (\text{job})$$

$$4x + 5x = 20$$

$$9x = 20$$

$$\boxed{x = 2\frac{2}{9} \text{ days}}$$

Example 3. A painter works on a job for 10 days and is then joined by his associate. Together they finish the job in 6 more days. The associated would have done the job alone in 30 days. How long would it take the painter alone to do the job?

	(per day)	\cdot	(on job)	$=$	w
painter	$\frac{1}{x}$	\cdot	16	$=$	$\frac{16}{x}$
associate	$\frac{1}{30}$	\cdot	6	$=$	$\frac{1}{5}$

$$5x \left(\frac{16}{x} + \frac{1}{5} = 1 \right)$$

$$80 + x = 5x$$

$$80 = 4x$$

$$\boxed{20 \text{ days} = x}$$